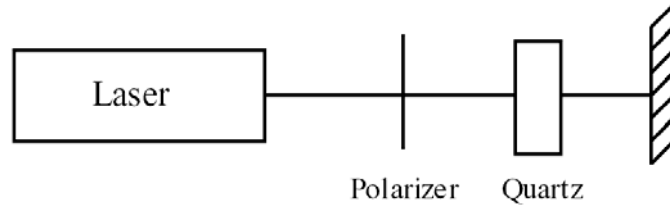


WP-C1) A quartz plate in the setup shown below has its axes at 45 degrees relative to the transmission axis of the linear polarizer. The indices of refraction for quartz are $n_o=1.544$ and $n_e=1.553$. The laser wavelength is 633 nm.

- What is the minimum quartz thickness for having no light reflected back to the laser?
- What is the minimum quartz thickness (other than zero) for having the maximum amount of light reflected back to the laser?

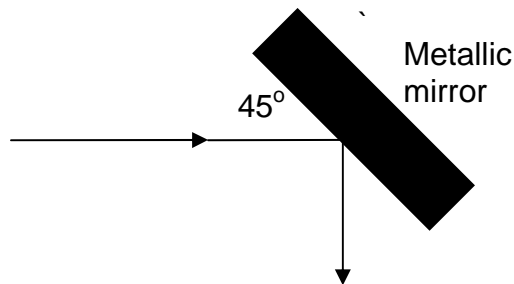


WP-C2) A left-hand circularly polarized laser beam illuminates the metallic mirror as shown below. The angle of incidence on the mirror is 45° . The Fresnel equations given below describe the reflection coefficient for s and p polarized light as a function of the angle of incidence, and the index of refraction of the metal is $N_t = 1.49+7.82j$. (This is the coefficient for Al at 650 nm).

- Draw the locus plot (trace of the tip of the electric vector in a plane perpendicular to the direction of propagation) for the electric vector after reflection from the mirror. (Hint: Use program `pol_locus_plot.m` after you have determined the state.)
- What is the state of polarization after reflection from the mirror? (Include a calculation of the ellipticity and the rotation angle θ of the major axis.

$$r_p = \frac{-N_t \cos \theta_i + N_i \cos \theta_t}{N_t \cos \theta_i + N_i \cos \theta_t}$$

$$r_s = \frac{N_i \cos \theta_i - N_t \cos \theta_t}{N_i \cos \theta_i + N_t \cos \theta_t}$$

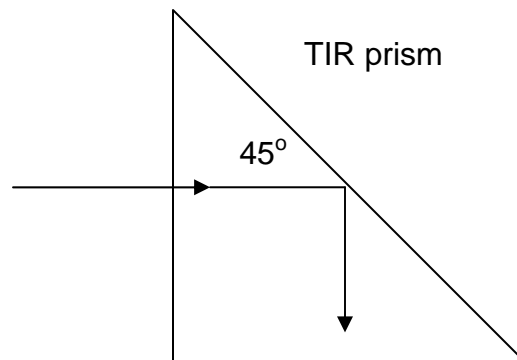


WP-C3) A left-hand circularly polarized laser beam illuminates the total-internal reflection prism as shown below. The angle of incidence on the turning surface is 45° . The Fresnel equations given below describe the reflection coefficient for s and p polarized light as a function of the angle of incidence, and the index of refraction of the glass is $N_i = 1.5$. Assume that the prism is in air with $N_t = 1$ and ignore effects of the entrance and exit surfaces of the prism.

- Draw the locus plot (trace of the tip of the electric vector in a plane perpendicular to the direction of propagation) for the electric vector after reflection from the turning surface. (Hint: Use program `pol_locus_plot.m` after you have determined the state.)
- What is the state of polarization after reflection from the turning surface? (Include a calculation of the ellipticity and the rotation angle θ of the major axis.)

$$r_p = \frac{-N_t \cos \theta_i + N_i \cos \theta_t}{N_t \cos \theta_i + N_i \cos \theta_t}$$

$$r_s = \frac{N_i \cos \theta_i - N_t \cos \theta_t}{N_i \cos \theta_i + N_t \cos \theta_t}$$



WP-C4) We showed in class that the complex index of refraction can be thought of as resulting from a classical mass-spring-damper system a form similar to:¹

¹ This is a little different form than what was presented in class.

$$N = \sqrt{1 + \frac{\text{constant}}{\omega_{01}^2 - \omega^2 - j2\omega\xi}} ,$$

where the constant contains terms related to the electronic charge, mass and molecular concentration. ω_{01} is the resonant frequency, ξ is the damping term, and ω is the driving frequency. Consider the case where the resonant wavelength is $0.3 \mu\text{m}$, constant = $3 \times 10^{31} \text{s}^{-2}$ and $\xi = 1.5 \times 10^{15} \text{s}^{-1}$. Graph the real and imaginary parts of the index of refraction for the wavelength range between $0.2 \mu\text{m}$ and $0.8 \mu\text{m}$.

WP-C5) A plane wave travels in air with direction cosines given by $(\alpha, \beta) = (0.3, 0)$. The maximum amplitude of the electric field is 1 V/m and the wavelength is $0.5 \mu\text{m}$.

- a.) Plot the electric field amplitude as a function of position along the line $(0, 0, z)$ for several periods of the wave at $t = 0$.
- b.) What is the velocity of the wave crest projection (peak of the electric field amplitude) that travels in this direction?

WP-C6) A $0.6328 \mu\text{m}$ wavelength spherical point source is used to approximate plane-wave illumination on a 1 mm diameter aperture. How far must the point source be located away from the aperture if the maximum allowed deviation from a plane wavefront is $1/100$ wave over the diameter of the aperture?

WP-C7) Two plane waves in air are traveling in the same direction. Wavelengths of the two waves in air are $\lambda_1 = 589.3 \text{ nm}$ and $\lambda_2 = 589.4 \text{ nm}$.

- a.) What is the beat frequency in Hz? Comment on the practicality of detecting this beat frequency if the maximum available detector bandwidth is 10^9 Hz .
- b.) What are the velocities of the modulation and high-frequency components?
- c.) If the waves travel in an optical glass with an Abbe number $V = 45$, does the answer to (b) change significantly?²

² The Abbe number V is a measure of the change of refractive index versus wavelength, where $V = (n_D - 1)/(n_F - n_C)$. n_D is the refractive index at $\lambda = 589.3 \text{ nm}$, n_F is the refractive index at $\lambda = 486.1 \text{ nm}$ and n_C is the refractive index at $\lambda = 656.3 \text{ nm}$.