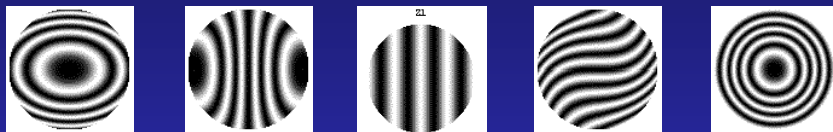


# Dynamic Interferometry



Neal Brock, John Hayes, and James Millerd

4D Technology

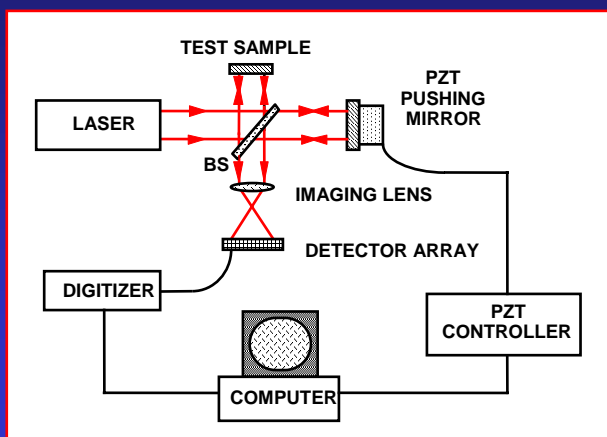
and

James C. Wyant

Optical Sciences Center

University of Arizona

# Phase-Shifting Interferometer



## Four Step Method

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$$I(x,y) = I_{dc} + I_{ac} \cos[\phi(x,y) + \overset{\text{phase shift}}{\phi(t)}]$$

**measured object phase**

$$\begin{aligned} I_1(x,y) &= I_{dc} + I_{ac} \cos [\phi (x,y)] & \phi (t) &= 0 & (0^\circ) \\ I_2(x,y) &= I_{dc} - I_{ac} \sin [\phi (x,y)] & &= \pi/2 & (90^\circ) \\ I_3(x,y) &= I_{dc} - I_{ac} \cos [\phi (x,y)] & &= \pi & (180^\circ) \\ I_4(x,y) &= I_{dc} + I_{ac} \sin [\phi (x,y)] & &= 3\pi/2 & (270^\circ) \end{aligned}$$

$$\mathbf{Tan}[\phi(x,y)] = \frac{I_4(x,y) - I_2(x,y)}{I_1(x,y) - I_3(x,y)}$$

## Serious Problem in Interferometry

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**Vibration!!**

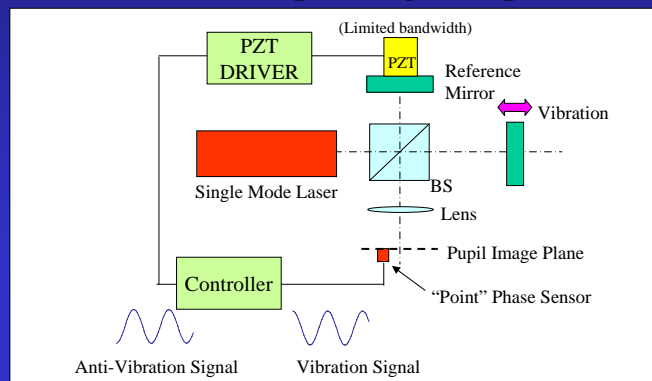
**Vibration is often the limiting factor  
in interferometry applications**

## Best Way to Fix Vibration Problem

- Retrieve frames faster
- Control environment
- Common-path interferometers
- Measure vibration and introduce vibration 180 degrees out of phase to cancel vibration
- Grab all frames at once (Single Shot)
- Carrier Frequency
- Pixelated Array

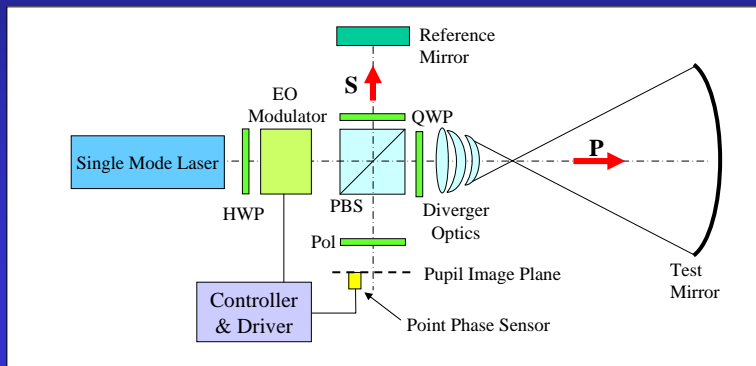
## Vibration Compensation Concept

- Example: Twyman-Green configuration
  - Sense optical phase
  - Feed back out-of-phase signal to phase shifter

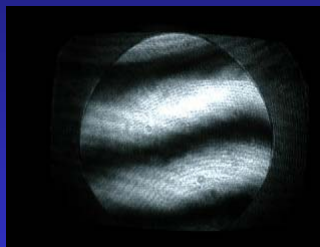


# Achieving High Speed Phase Modulation

- Use polarization Twyman-Green configuration
- EOM changes relative phase between 'S' & 'P' components
  - Can be very fast: 200 kHz - 1 GHz response



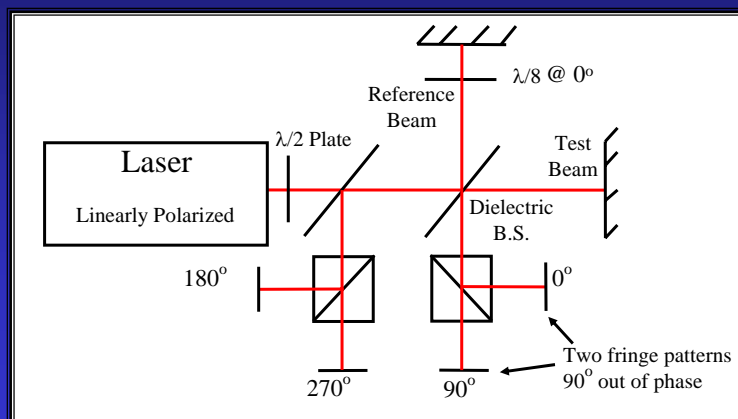
## Results



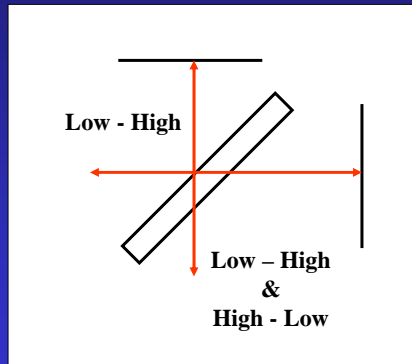
## Conclusions - Active Vibration Cancellation Interferometer

System works amazingly well,  
but it is rather complicated  
and expensive.

## Simultaneous Phase-Measurement Interferometer

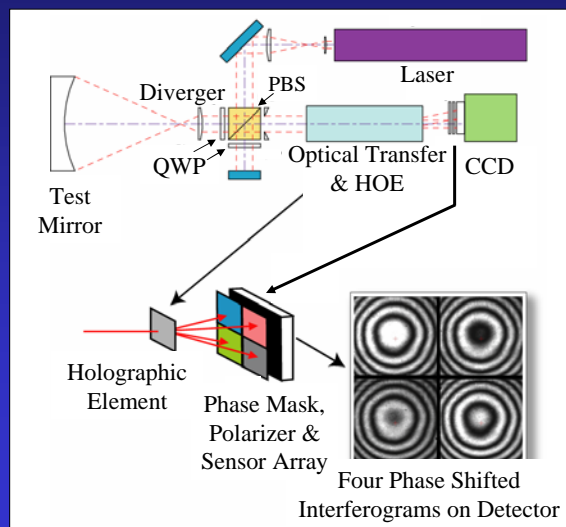


## Dielectric beamsplitter and phase shift upon reflection for test and reference beams



## 4D PhaseCam Operation

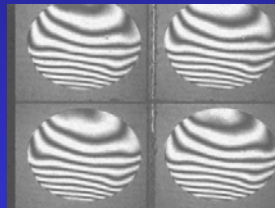
- **Twyman-Green**
  - Two beams have orthogonal polarization
- **4 Images formed**
  - Holographic element
- **Single Camera**
  - 1024 x 1024
  - 2048 x 2048
- **Polarization used to produce 90-deg phase shifts**



## Effects of Vibration



*Relative motion  
between PhaseCam  
and test object*

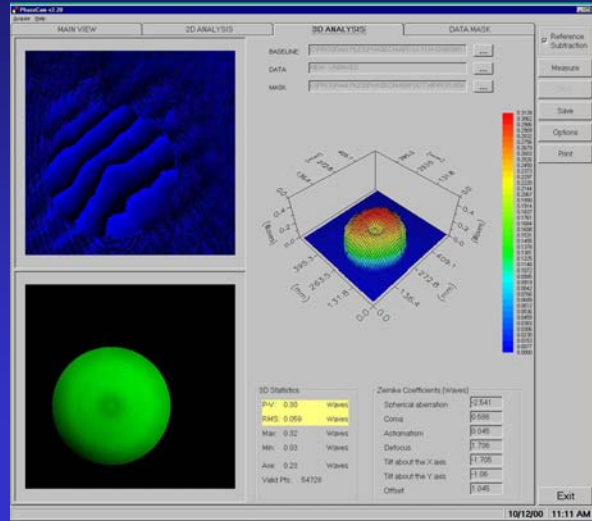


*Phase relationship is fixed*

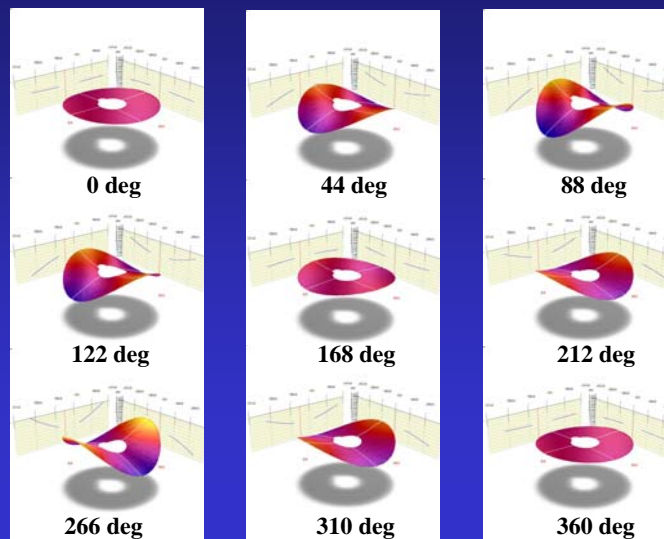
## Testing a 0.5 meter diameter, 20 meter ROC mirror



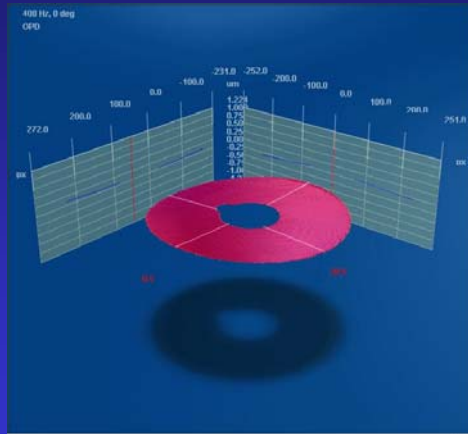
# 0.5 m diameter mirror, 20 m ROC 5 nm rms repeatability (in air)



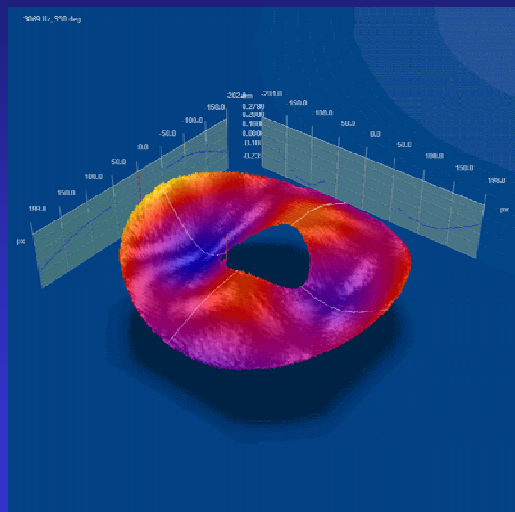
# Phase Sweep at 408 Hz



## Hard Disk Platter Excited by PZT at 408 Hz



## Hard Disk Platter Excited by PZT at 3069 Hz

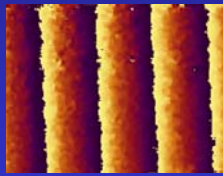


# Surface Subtraction

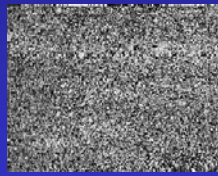
Subtraction in interferogram domain (diffuse and specular surfaces)

*Stetson - 8 frame phase-difference*

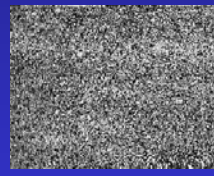
$$\Delta Z = \frac{\lambda}{2} \operatorname{atan} \left( \frac{[D_0 - B_0][A(t) - C(t)] - [A_0 - C_0][D(t) - B(t)]}{[A(t) - C(t)][A_0 - C_0] + [D_0 - B_0][D(t) - B(t)]} \right)$$



+  
Unwrapping



A(t), B(t), C(t), D(t)



A<sub>0</sub>, B<sub>0</sub>, C<sub>0</sub>, D<sub>0</sub>

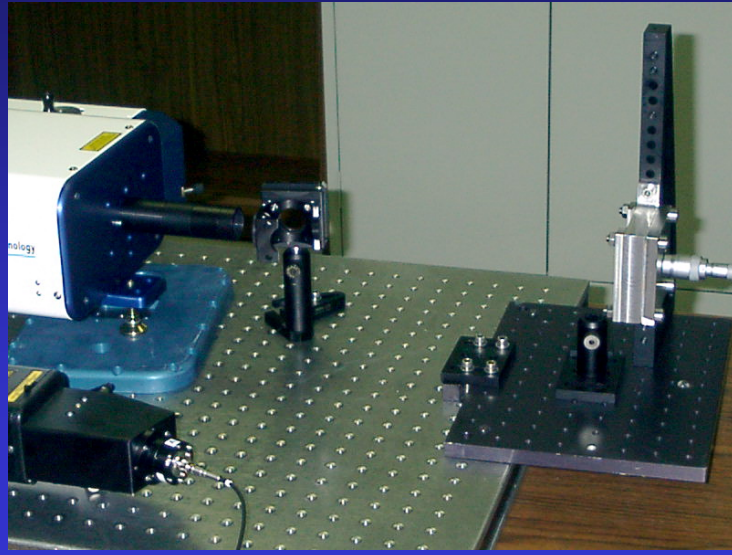
• *Not necessary to solve for random phase*

# Backplane Deformation Holder



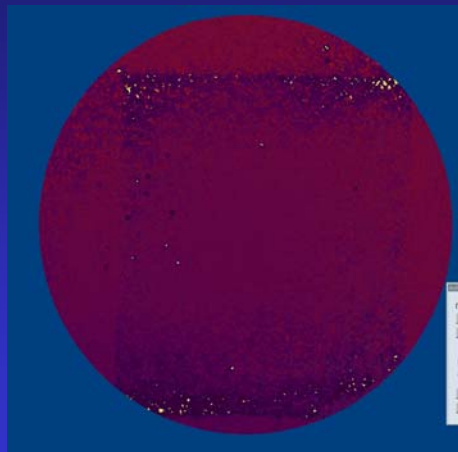
## Set Up for Backplane Deformation Measurement

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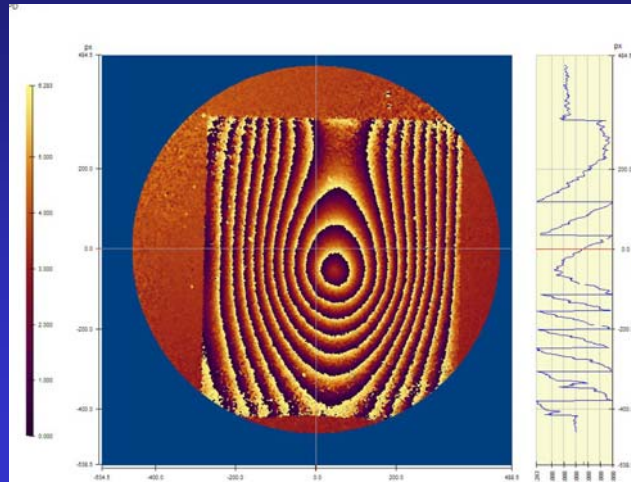
## Backplane

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## Carbon Fiber Deformation

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(Metrology for JWST Backplane)

## Conclusions – Single Shot Interferometer

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- Vibration insensitive, quantitative interferometer
- Surface figure measurement (nm resolution)
- Snap shot of surface height
- Acquisition of “phase movies”

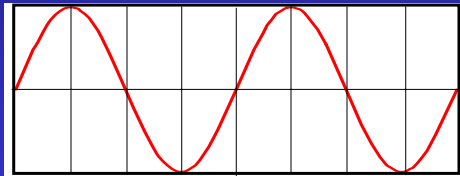
Still not perfect

Not easy to use multiple wavelength  
or white light interferometry

## **N-Point Technique (Carrier Frequency)**

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**Phase shifting algorithms applied to consecutive pixels thus requires calibrated tilt**



**4 pixels per fringe for 90 degree phase shift**

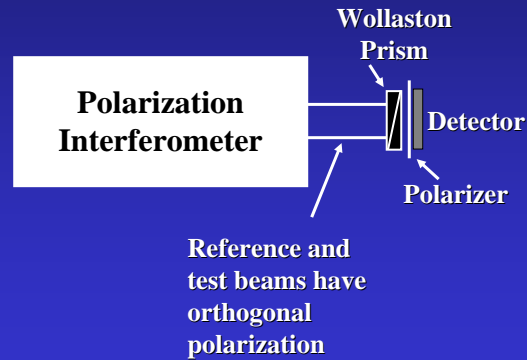
## **Creating the Carrier Frequency**

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- **Introduce tilt in reference beam**
  - Aberrations introduced due to beam transmitting through interferometer off-axis
- **Wollaston prism in output beam**
  - Requires reference and test beams having orthogonal polarization
- **Pixelated array in front of detector**
  - Special array must be fabricated

## Use of Wollaston Prism to Produce Carrier Fringes

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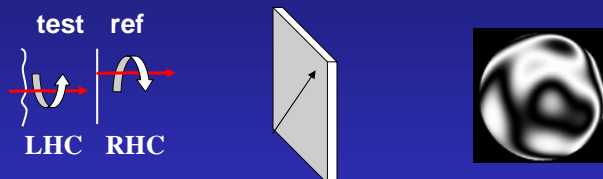


## Pixelated Phase Sensor

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- **Compacted pixelated array placed in front of detector**
- **Single frame acquisition**
  - High speed and high throughput
- **Achromatic**
  - Works from blue to NIR
- **True Common Path**
  - Can be used with white light

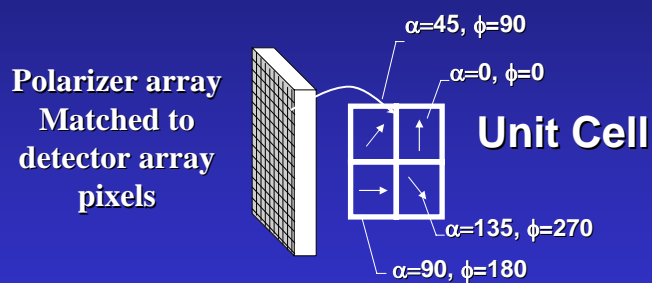
## Use polarizer as phase shifter



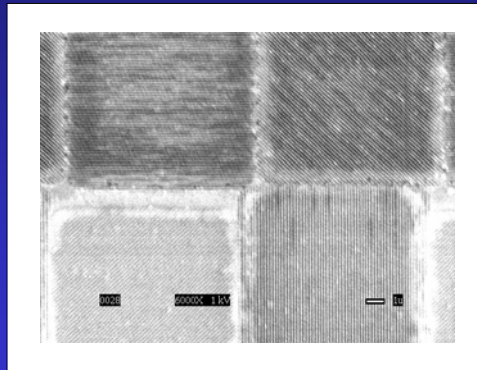
Circ. Pol. Beams ( $\Delta\phi$ ) + linear polarizer ( $\alpha$ )  $\longrightarrow$   $\cos(\Delta\phi + 2\alpha)$

*Phase-shift depends on polarizer angle*

## Array of oriented micropolarizers

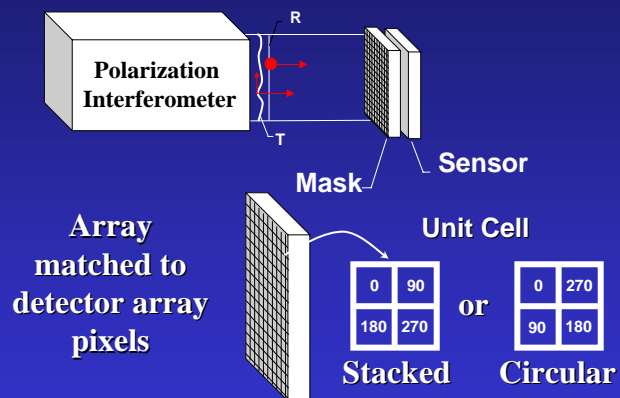


## Electron micrograph of wire grid polarizers



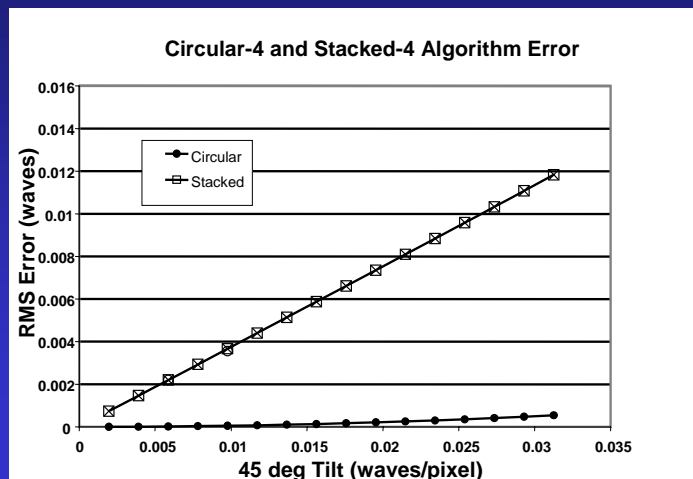
← 20 um →

## Array of phase-shift elements unique to each pixel

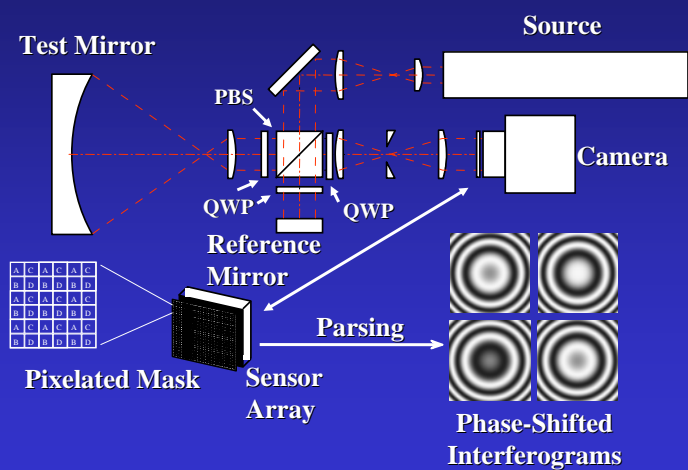


- Similar to spatial carrier but
  - true common path
  - fixed carrier period

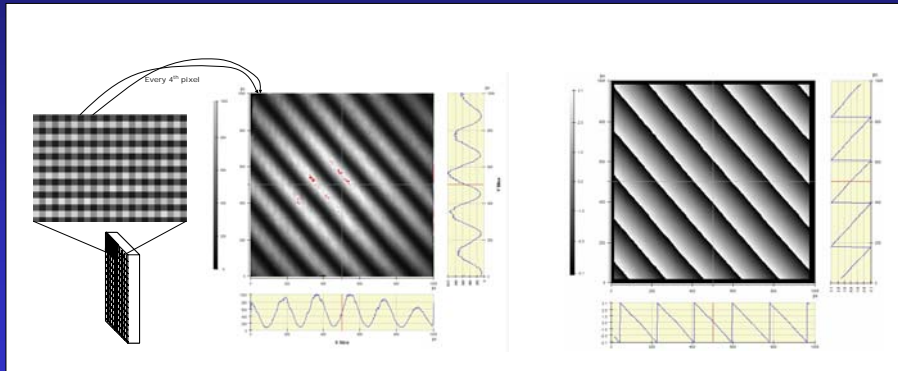
# Phase error vs fringe tilt



# System Configuration



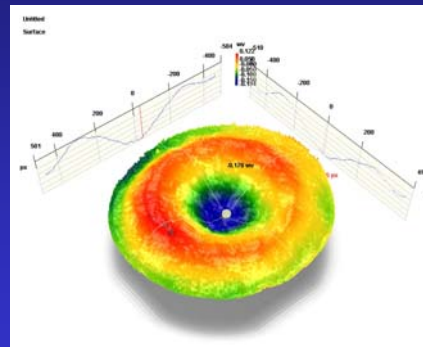
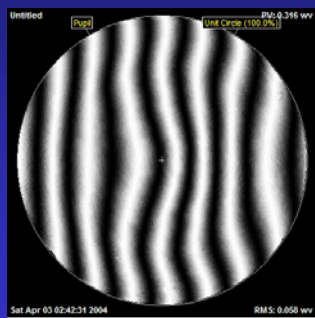
# Measurements



Fringe pattern synthesized by selecting every fourth pixel.

Phase map.

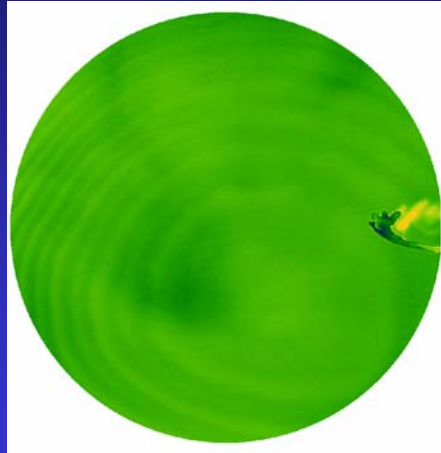
## Measurement of 300 mm diameter, 2 meter ROC mirror



Mirror and interferometer on separate tables!

## Measurement Results

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Air burst  
Phase w/reference subtraction

## Pixelated Phase Sensor Advantages

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- Single frame acquisition
  - High speed and high throughput
- Achromatic
  - works from blue to NIR
- True Common Path
  - Can be used with white light
- Fixed Carrier
  - Faster processing and calib.
- Compact
  - no bigger than camera
- Versatile
  - can be interfaced to many interferometer configurations

**Thank you!**

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