

# Infrared Optical Systems

OPTI 696

Practical Optics Seminar

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Raytheon Missile Systems

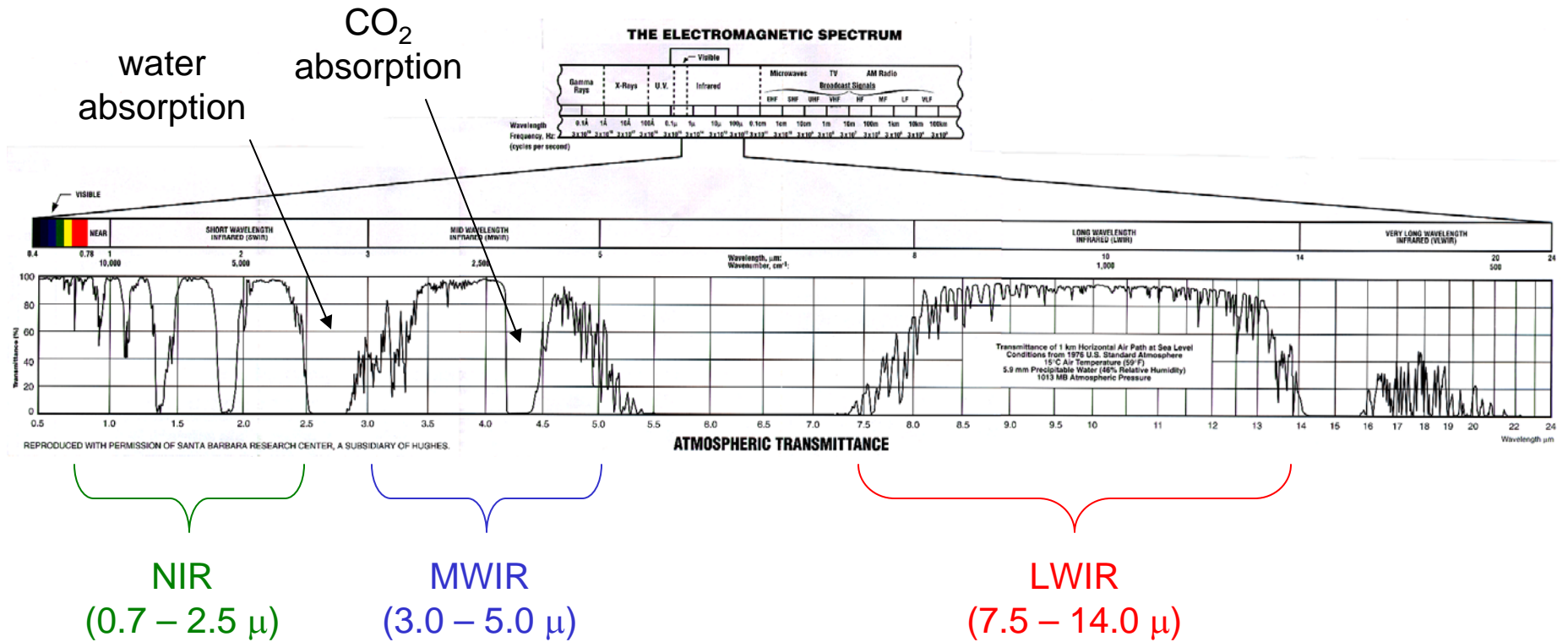
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# Atmospheric Transmittance



# Blackbody Radiation

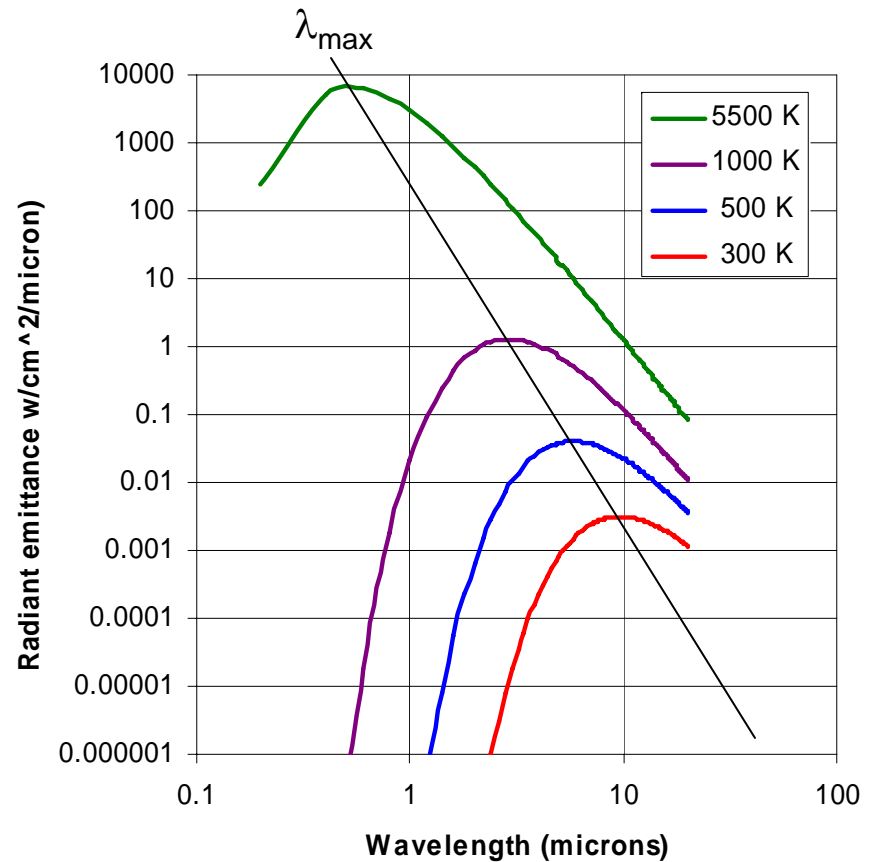
- Blackbodies emit per the following equation

$$W(\lambda) = \frac{C_1}{\lambda^5 (e^{C_2/\lambda T} - 1)}$$

$$C_1 = 2\pi c^2 h = 37418.32 \text{ w}\mu^4\text{cm}^{-2}$$

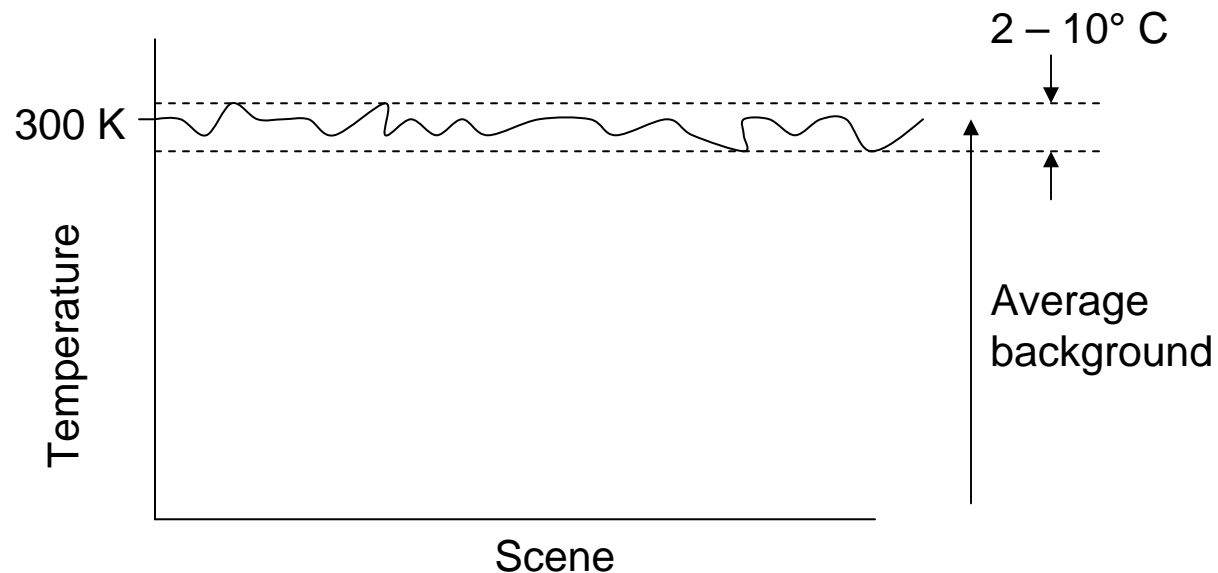
$$C_2 = hc/k = 14387.86 \mu\text{K}$$

- The peak of the curve occurs at  
 $\lambda_{\text{max}} = 2898/T$ 
  - Visible (T = 5500)  $\lambda_{\text{max}} = 0.53 \mu$
  - MWIR (T = 500)  $\lambda_{\text{max}} = 5.8 \mu$
  - LWIR (T = 300)  $\lambda_{\text{max}} = 9.7 \mu$
- The choice of spectral band to use depends on the temperature of the object you want to detect



# Thermal Contrast

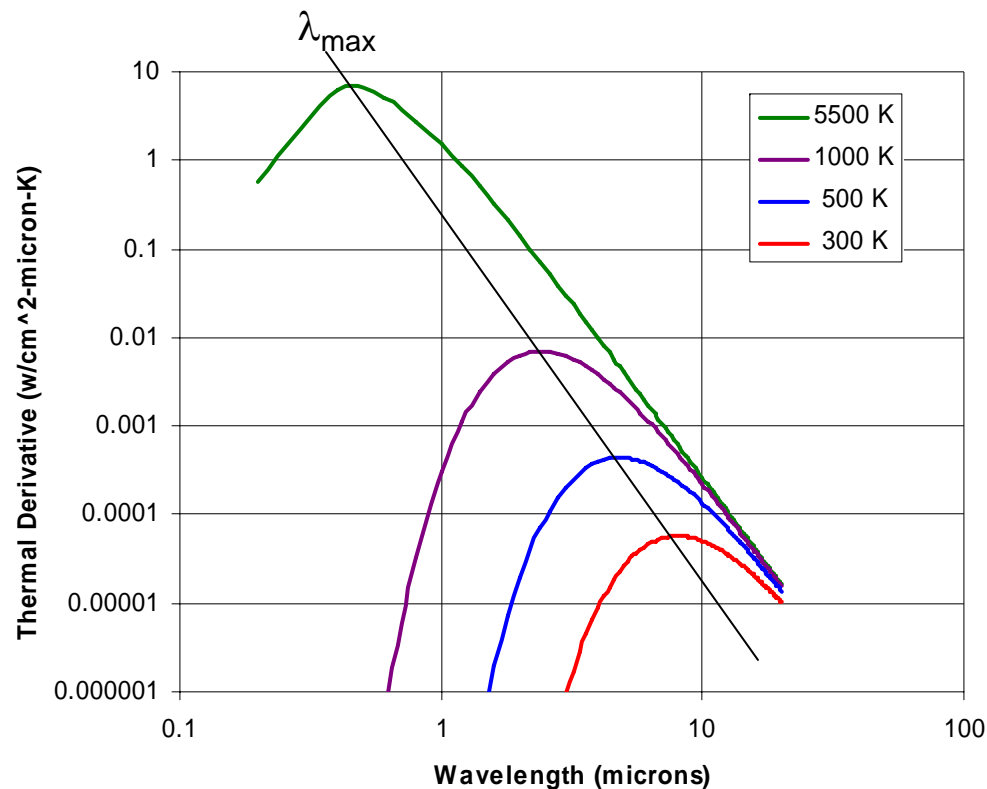
- Terrestrial objects are at about 300 K ( $\sim 25^\circ\text{C}$ )
  - The human body, for example, has a thermal contrast of about  $3 - 8^\circ\text{C}$
- Thus, a typical IR scene has a contrast of only a few percent (as opposed to visible scenes, which have 100% contrast)
- To maintain the dynamic range in the important part of the image, the background is usually subtracted out



# Blackbody Thermal Derivative

- Since the background is subtracted from the IR scene, the sensor really detects the change in temperature, or the thermal derivative  $\partial W/\partial T$

$$\frac{\partial W}{\partial T} = \frac{c_1 c_2 e^{c_2/\lambda T}}{\lambda^6 T^2 (e^{c_2/\lambda T} - 1)^2}$$

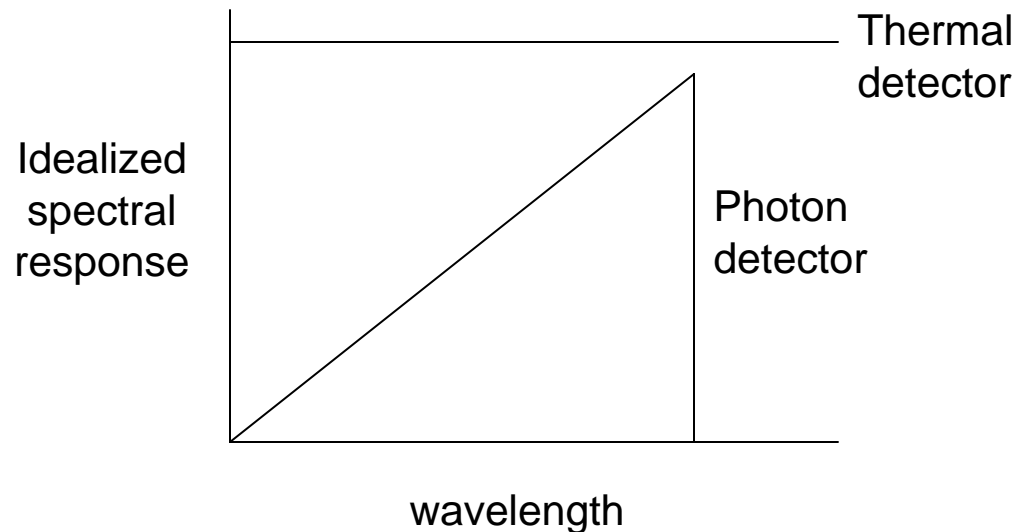


Peak wavelength  
is at  $\lambda_{\max} = 2410/T$

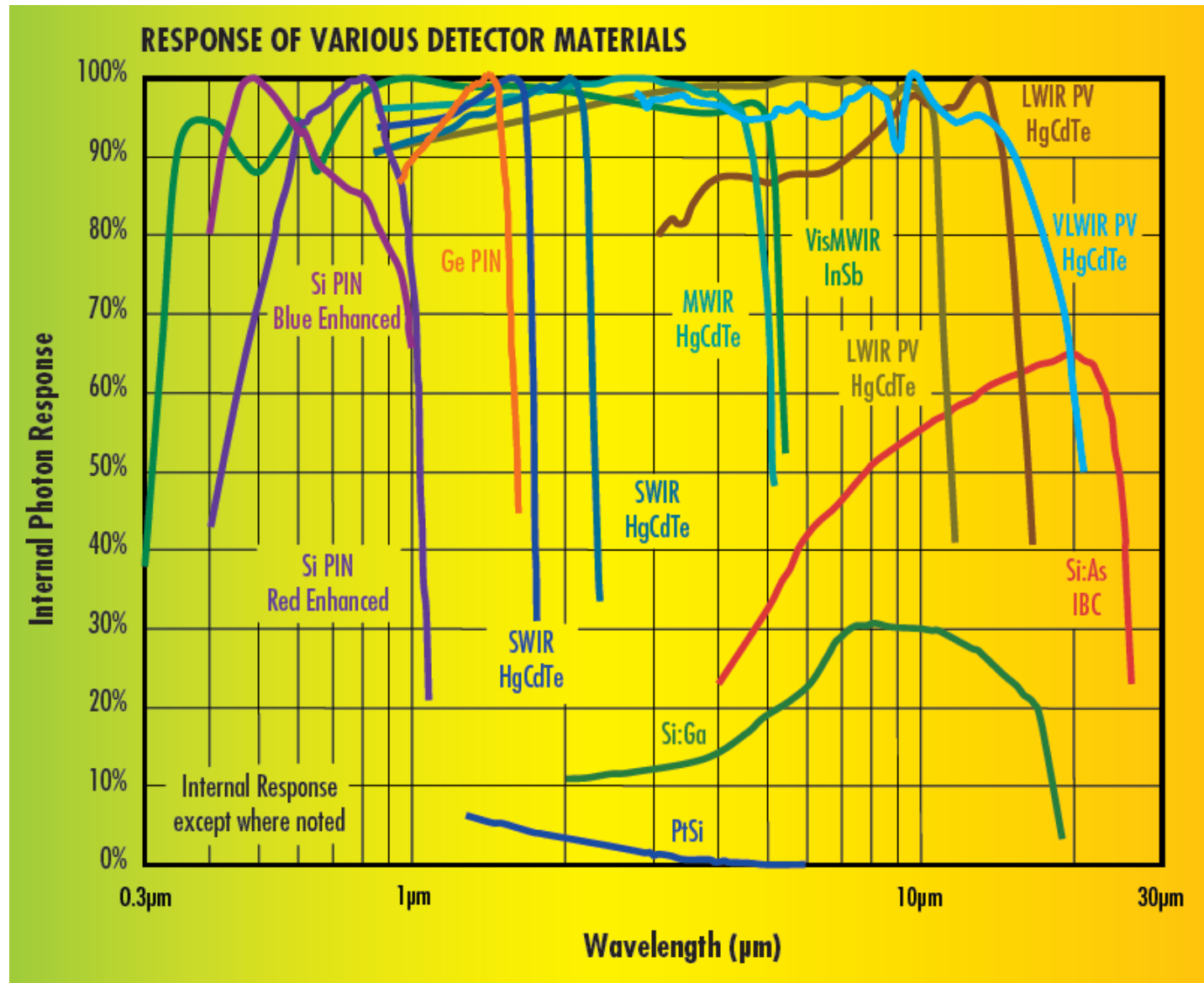
# IR Detectors

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- Two kinds of IR detectors
  - Thermal detectors – sense temperature
  - Photon detectors – sense photon energies
- Thermal detectors have a flat spectral response with wavelength
- Photon detectors have a spectral response proportional to wavelength with a peak wavelength (related to material properties such as band gaps) beyond which there is little or no response



# Infrared Detectors



# IR Signal

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- The total signal received by the detectors is the product of the target spectral emission, the atmospheric transmittance, the optical transmittance, and the detector spectral response

$$\text{Signal} = \int E_{\text{target}}(\lambda) \tau_{\text{atmosphere}}(\lambda) \tau_{\text{optics}}(\lambda) R_{\text{detector}}(\lambda) d\lambda$$

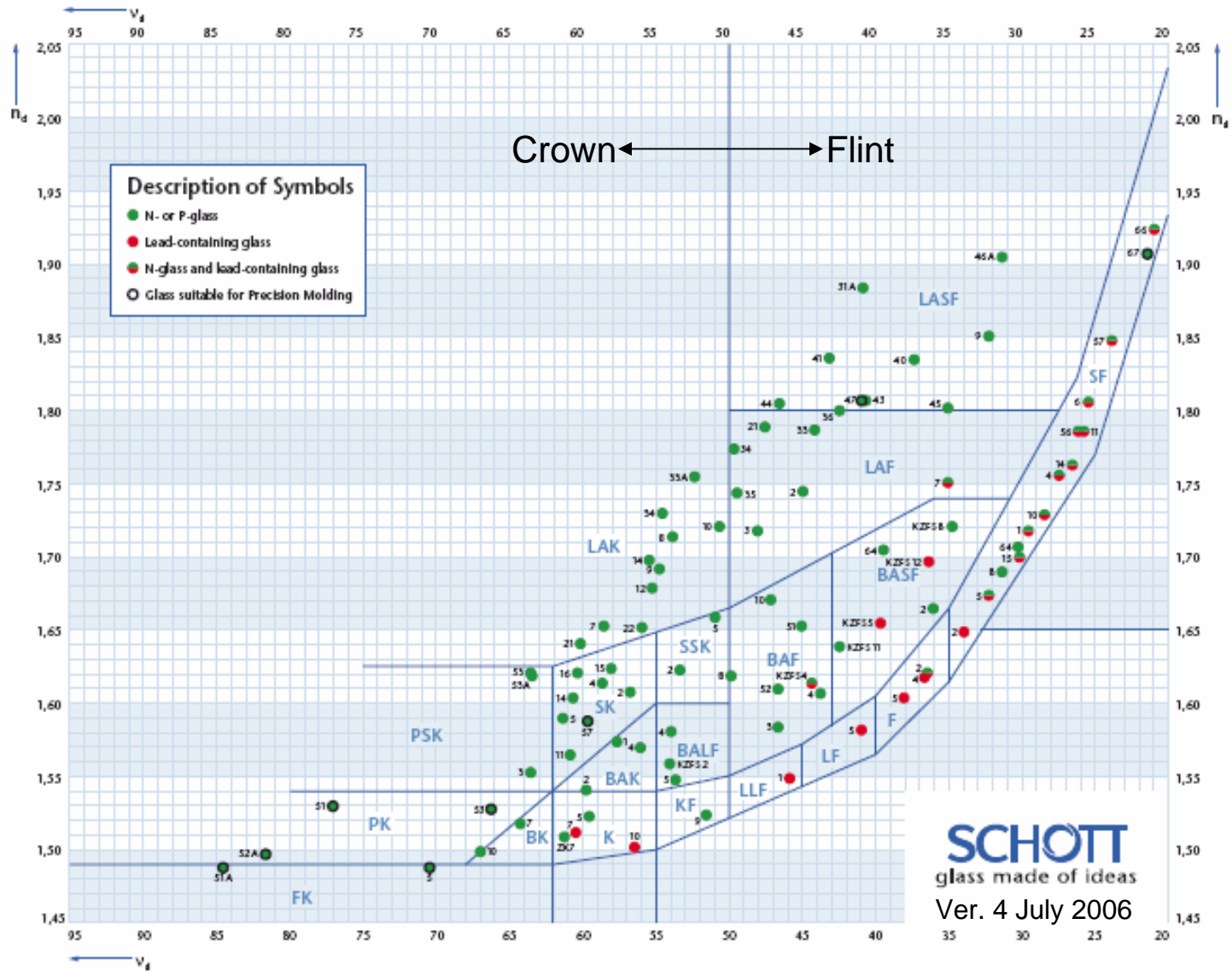
- Of course, there's also the radiometric factors such as target size, solid angles, f/numbers, detector size, etc., which we will not go into here
- We are also ignoring for this seminar the noise contributions such as thermal background, detector noise, electronic noise, etc.

# Infrared Glasses vs. Visible Glasses

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- IR glasses have significantly higher refractive indices
  - Visible glass –  $n$  ranges between 1.45 and 2.0
  - IR glasses –  $n$  ranges between 1.38 to 4.0
- Dispersion can be significantly lower (depending on spectral band)
  - Visible glasses –  $V$  ranges from 20 to 80
  - IR glasses –  $V$  ranges from 20 to 1000
- Many IR glasses are opaque in the visible
  - And most visible glasses are opaque in the IR
- IR glasses are often heavier than visible glasses
- IR glasses have significantly higher  $dn/dT$  values (factor of 10 or more higher)
- IR glasses cost more than visible glasses (by 2 or more orders of magnitude)
- Significantly fewer number of practical IR glasses than visible glasses

# Visible Glass Map



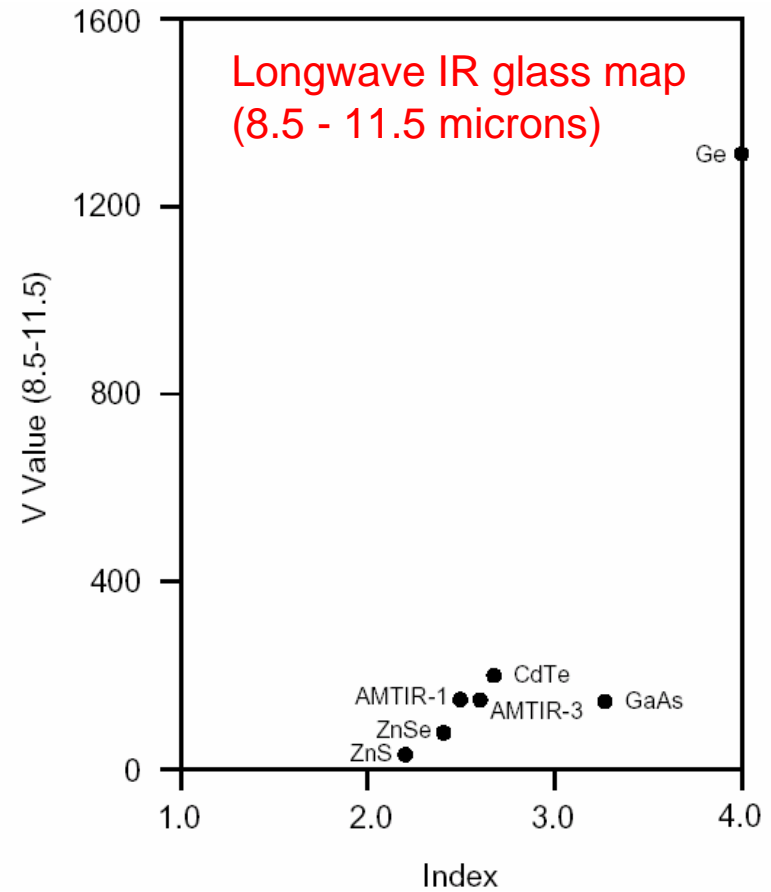
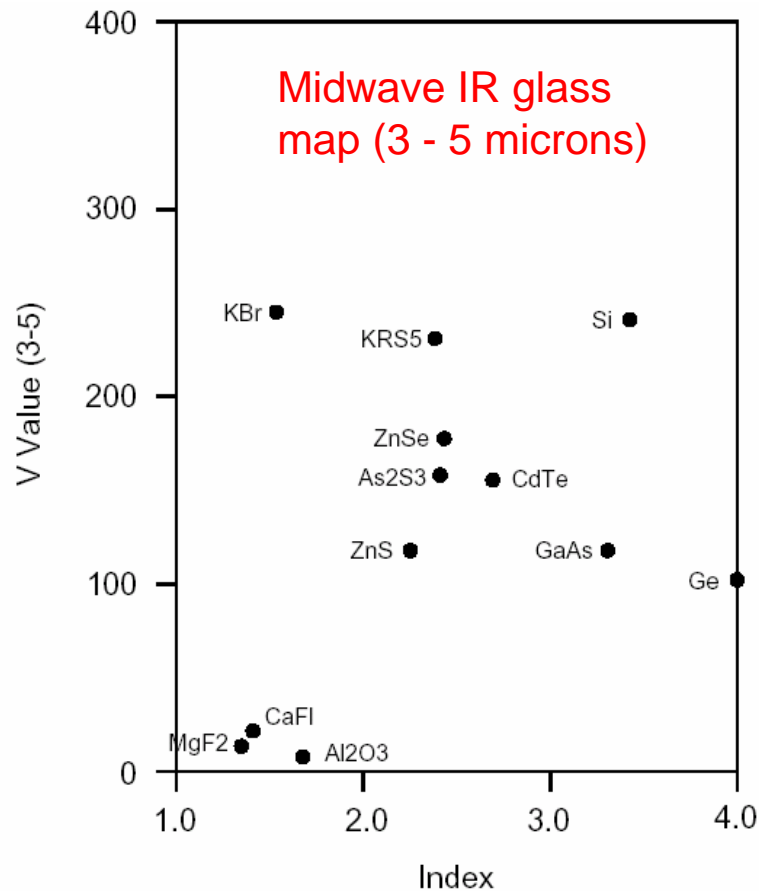
# Infrared Glasses

- The list of commonly used IR materials is (unfortunately) pretty short

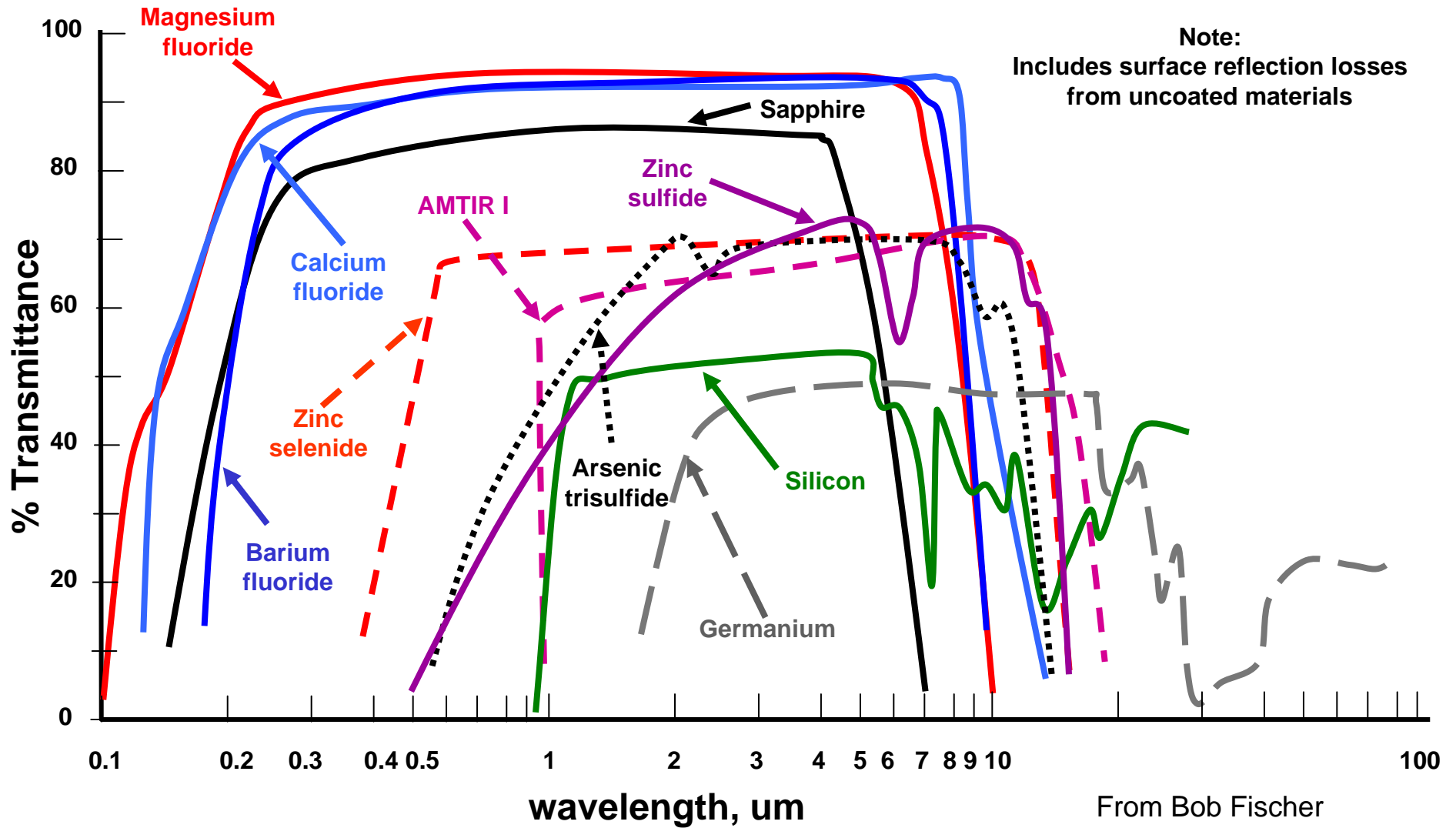
Germanium  
Silicon  
Zinc Sulfide

AMTIR 1, 3  
Sapphire  
Zinc Selenide

Magnesium Fluoride  
Gallium Arsenide  
Calcium Fluoride



# Transmittance of IR glasses



From Bob Fischer

# Designing With IR Glasses

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- Advantages 😊

- Refractive index is usually higher, so fewer lenses are needed to achieve diffraction-limited performance
- Dispersion is often low enough such that color correction may not be necessary
- Most IR materials can be diamond point machined, so aspherics are commonly used in designs
- The Airy disk size and diffraction-limited depth of focus are larger for the IR than for the visible, so achieving diffraction-limited performance is easier

- Disadvantages ☹️

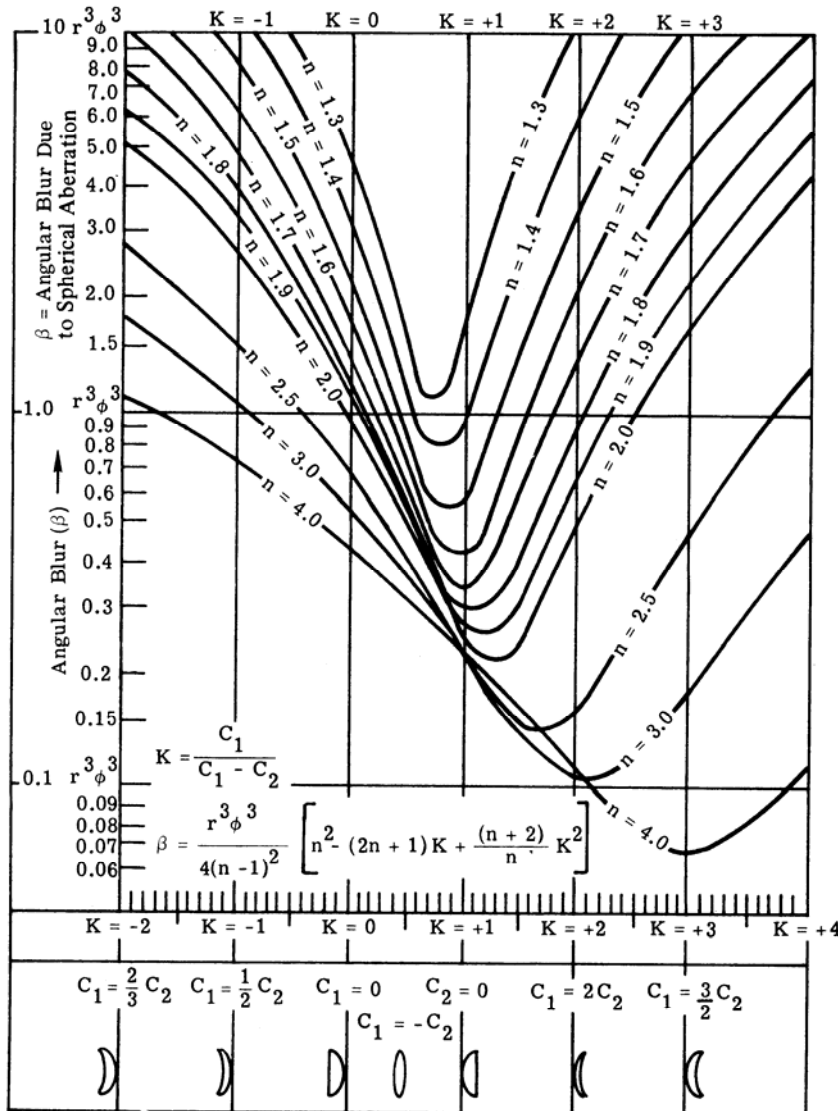
- Small choice of glasses
- Materials are expensive (~1\$/gram)
  - One-inch diameter BK7 lens \$5
  - One-inch diameter germanium lens \$500
  - Five-inch diameter sapphire dome Priceless
- Some IR materials are difficult to fabricate and/or antireflection coat
  - Fragile, soft, chip easily, low thermal conductivity, etc.
- Most IR materials have large  $dn/dT$  values, so athermalizing can be difficult

# Cautions on IR Glasses and Optics Software

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- There is only one source of data on Schott glasses – Schott Optical Glass
- However, there is no "source" of data on IR glasses
- Most optical software programs depend on some literature source of data for IR materials, then fit the data to Sellmeier equations
  - Some programs do a better job of this than others
- Some IR glasses, such as AMTIR, are made by a specific supplier who publishes index data on the material
  - Sometimes these data are not consistent, come from different measurement sources, and may not have sufficient significant digits
  - In these cases, if your design is sensitive to the glass dispersion, you may need to double-check the index data
- Thermal data, such as thermal expansion coefficient and  $dn/dT$  data may vary widely for some materials, depending on who measured it
  - Usually, optical software do not include these data, as there is no official "source" for these data

# Spherical Aberration vs. Refractive Index



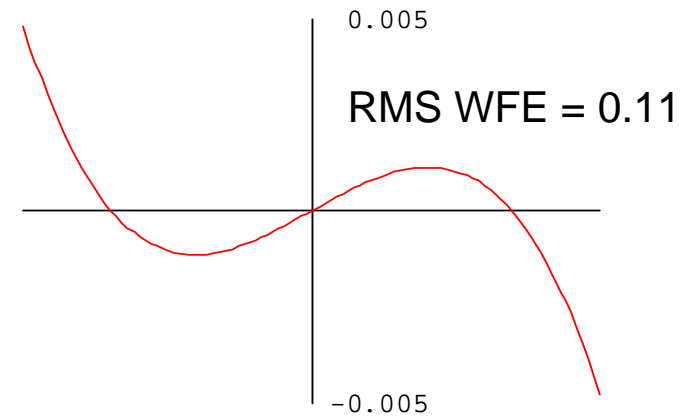
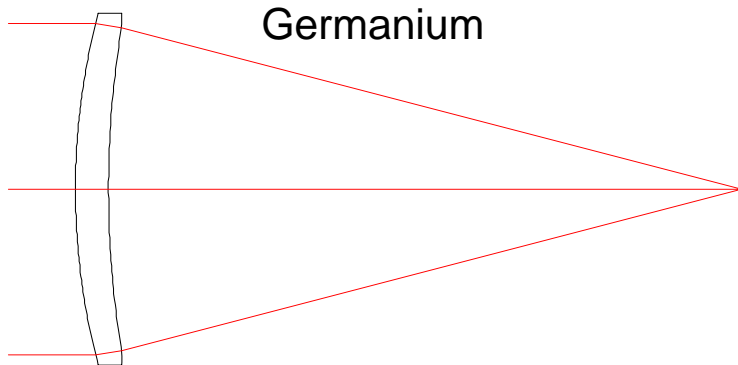
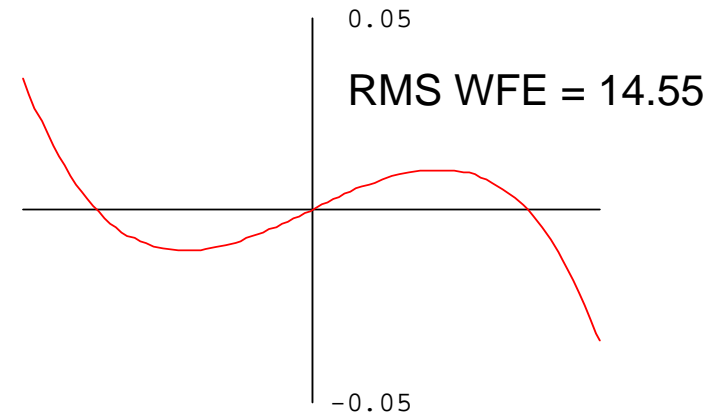
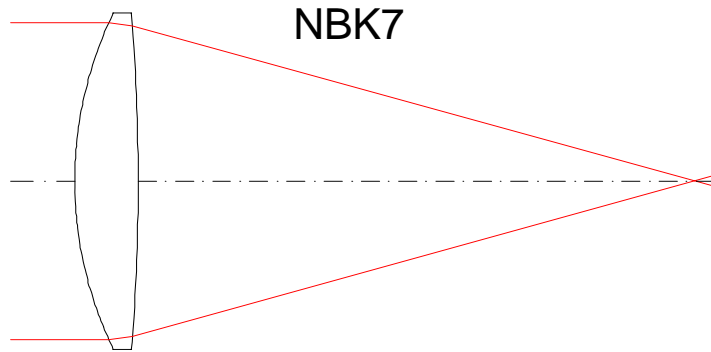
$$K_{\min} = \frac{n(2n+1)}{2(n+2)}$$

$$\beta \text{ at } K_{\min} = r^3 \phi^3 \frac{4n^2 - n}{16(n-1)^2(n+2)}$$

For germanium  $n = 4$

$$\beta = \frac{0.0087}{f^3}$$

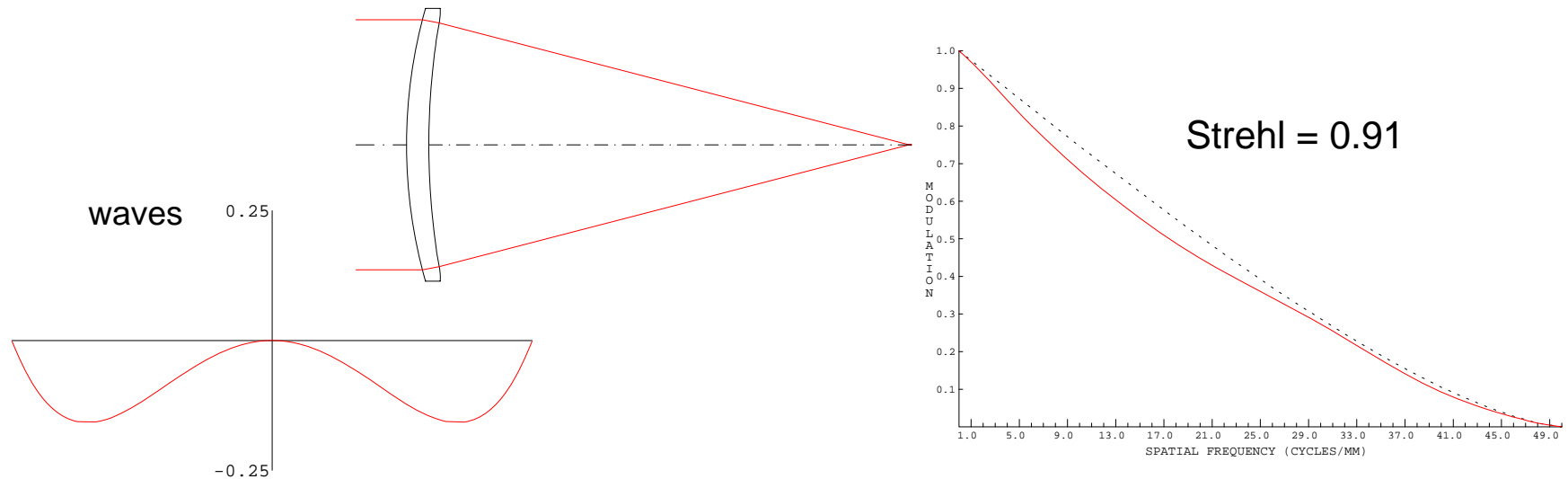
# NBK7 vs. Germanium – Spherical Aberration



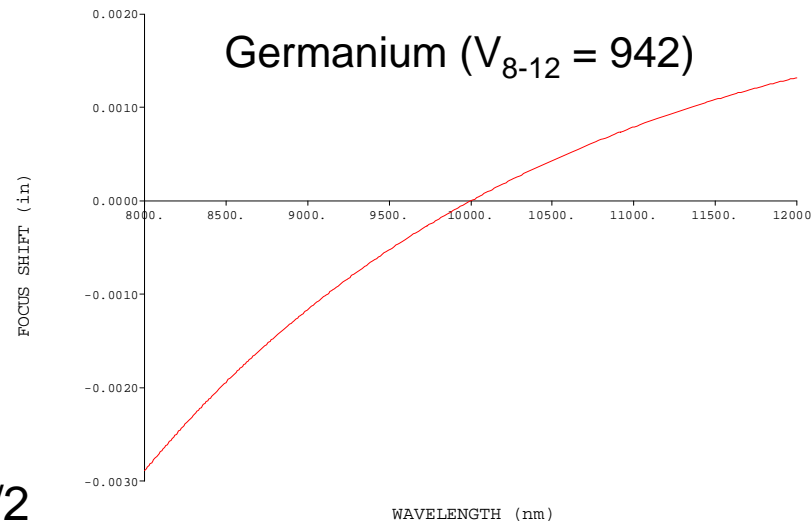
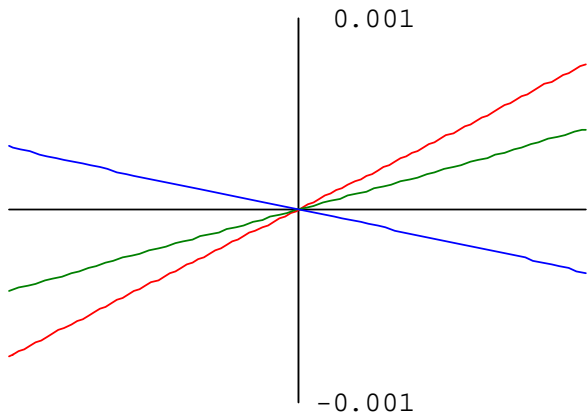
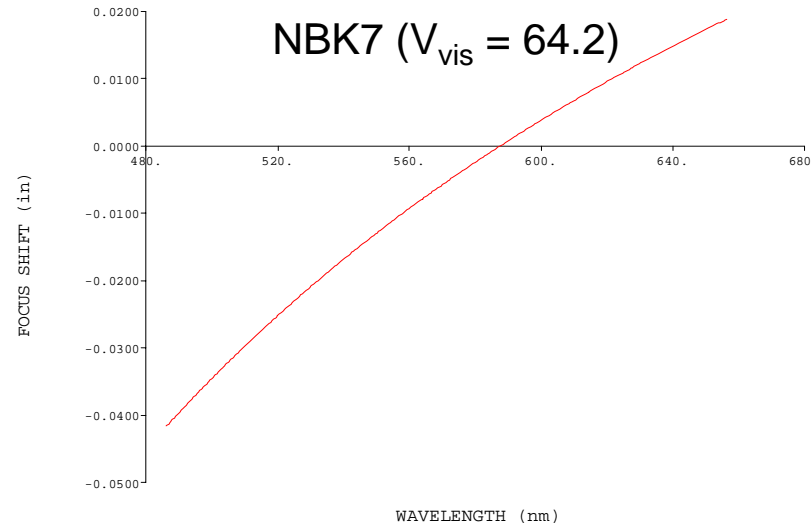
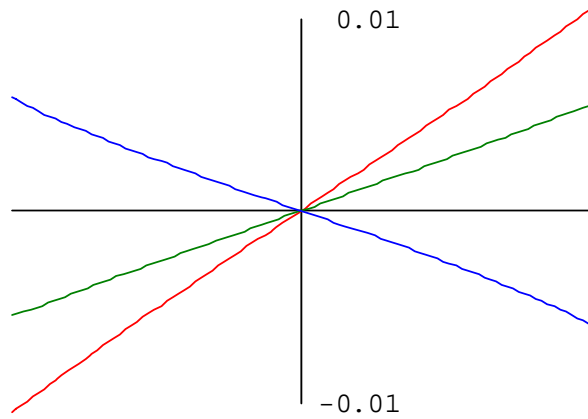
4.0 inch EFL, f/2

# Example - Germanium Singlet

- We want an f/2 germanium singlet to be used at 10 microns (0.01 mm)
- Question - What is the longest focal length we can have and not need aspherics to correct spherical aberration?
- Answer
  - Diffraction Airy disk angular size is  $\beta_{\text{diff}} = 2.44 \lambda/D$
  - Spherical aberration angular blur is  $\beta_{\text{sa}} = 0.0087 / f^3$
  - Equating these gives  $D = 2.44 \lambda f^3 / 0.0087 = 22.4 \text{ mm}$
  - For f/2, this gives  $F = 45 \text{ mm}$



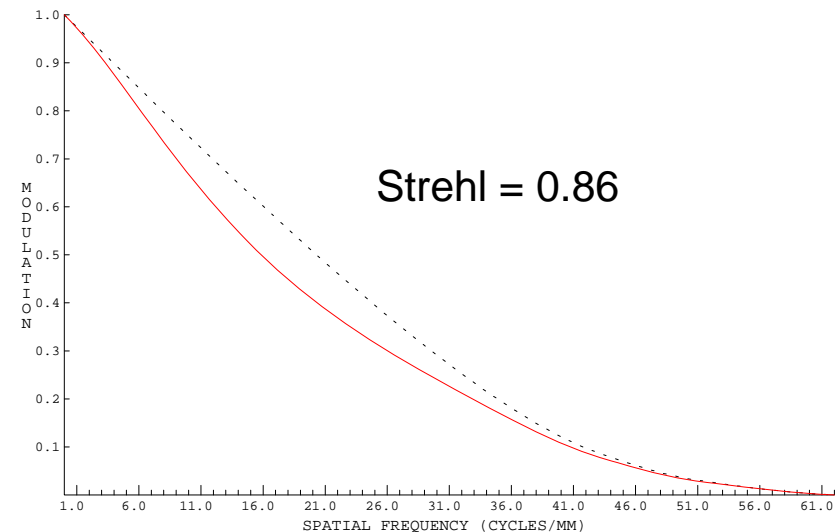
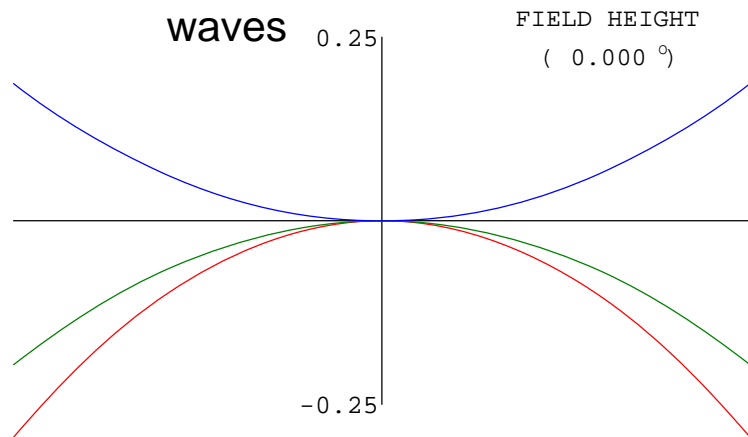
# NBK7 vs. Germanium – Chromatic Aberration



4.0 inch EFL, f/2

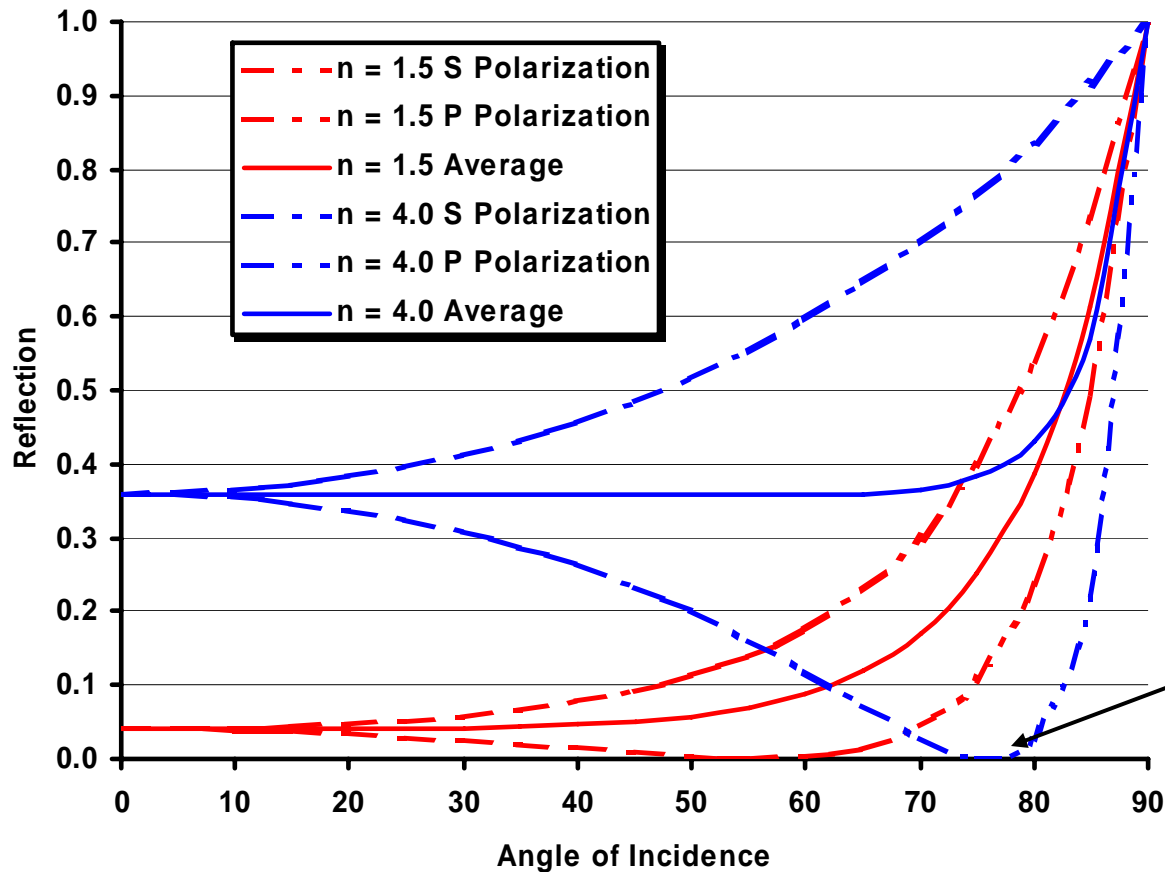
# Chromatic Aberration Example - Germanium Singlet

- We want to use an f/2 germanium singlet over the 8 to 12 micron band
- Question - What is the longest focal length we can have and not need to color correct? (assume an aspheric to correct any spherical aberration)
- Answer
  - Over the 8-12 micron band, for germanium  $V = 942$
  - The longitudinal defocus =  $F / V = F / 942$
  - The 1/4 wave depth of focus is  $\pm 2\lambda f^2$
  - Equating these and solving gives  $F = 4 * 942 * \lambda * f^2 = 150 \text{ mm}$



# Surface Reflection

- Bare glass reflects a portion of the light hitting it
  - The amount reflected depends on the index of the glass, the angle of incidence of the light, and the polarization of the light



$$R_S = \frac{\sin^2(\theta - \theta')}{\sin^2(\theta + \theta')}$$

$$R_P = \frac{\tan^2(\theta - \theta')}{\tan^2(\theta + \theta')}$$

Brewster's angle =  $\tan^{-1}n$

# Single Layer Anti-reflection Coating

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- The single layer is the simplest anti-reflection (AR) coating
- Let the incident medium be  $n_0$  (usually air, so  $n_0 = 1$ ), the index of the coating be  $n_1$ , and the index of the substrate be  $n_2$
- The reflectivity of the surface for an incident angle  $\theta$  is

$$R = \frac{r_1^2 + r_2^2 + 2r_1r_2 \cos X}{1 + r_1^2 r_2^2 + 2r_1r_2 \cos X} \quad \text{where} \quad X = \frac{4\pi n_1 t \cos \theta}{\lambda}$$

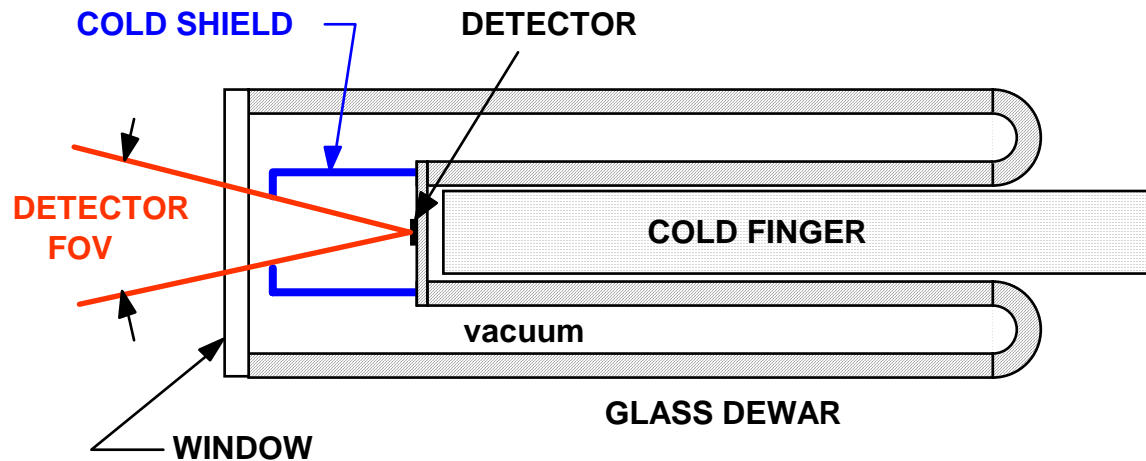
– R is minimized when  $\cos X = -1$ , or when  $n_1 t = \lambda/4$

- For normal incidence,  $r_1 = \frac{n_0 - n_1}{n_0 + n_1}$        $r_2 = \frac{n_1 - n_2}{n_1 + n_2}$

Then  $R = \left[ \frac{n_0 n_2 - n_1^2}{n_0 n_2 + n_1^2} \right]^2$       minimized when  $n_1 = \sqrt{n_0 n_2}$

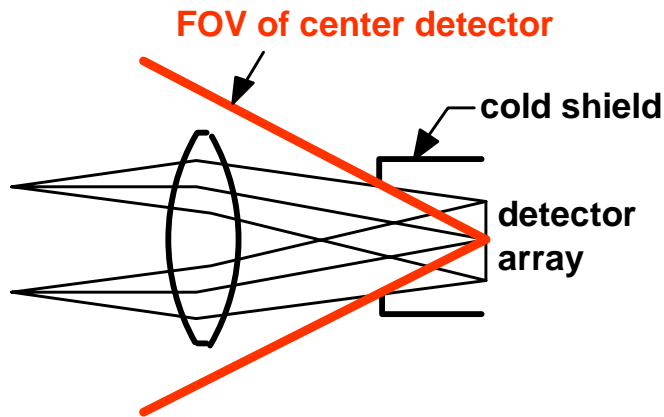
# Cooled Detectors

- Many IR systems require a cooled detector
  - Typically cooled to 77 K or lower (liquid nitrogen temperatures)
- To avoid frosting up, the detectors are mounted in a thermally insulated vacuum enclosure called a dewar
- Inside the dewar, a cold shield limits the angle of radiation which can be seen by the detector
  - This increases the detector sensitivity ( $D^*$ )

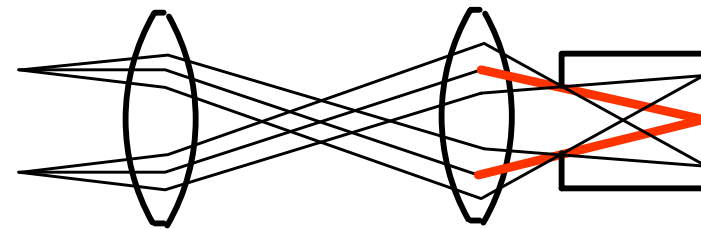


# Cold Shield Efficiency

- All IR systems with cooled detectors have a cold shield in the dewar to minimize the background radiation
  - The size of this cold shield determines the amount of background radiation seen by the detector and hence the system sensitivity



**Less than 100% cold shield efficiency  
(using simple imager)**



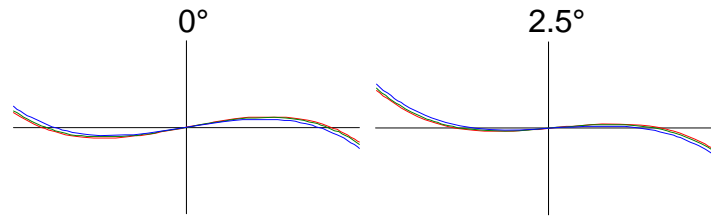
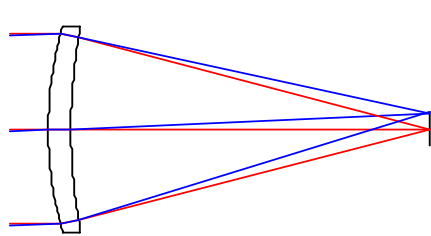
**100% cold shielding efficiency  
(using re-imaging imager)**

# Aperture Stop and Pupil Aberration

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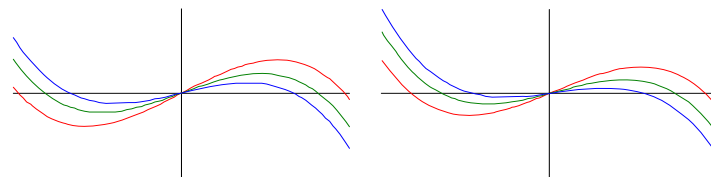
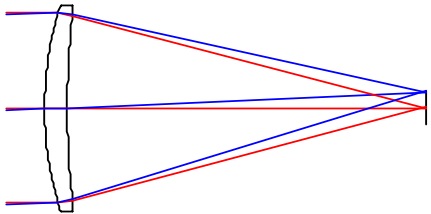
- The aperture stop is usually at one of two locations
  - On the front lens
  - At the cold shield
- Whichever one it is located at, it is often imaged onto the other to minimize its size
- Pupil aberration (spherical or coma of the pupil) usually causes the image of the stop to be oversized by about 10-15%
  - If the stop is at the front objective, this requires an enlarged cold shield
    - Result is lower detector sensitivity and lower system performance
  - If the stop is at the cold shield, this requires an oversized objective
    - This increases cost and weight

# Singlet Design Examples – f/2, 50 mm EFL (8 – 12 $\mu$ )



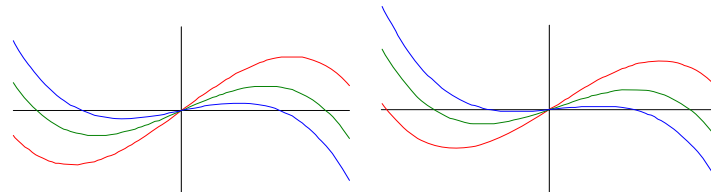
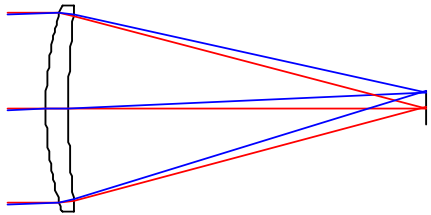
Germanium singlet (V=942)

RMS WFE = .096



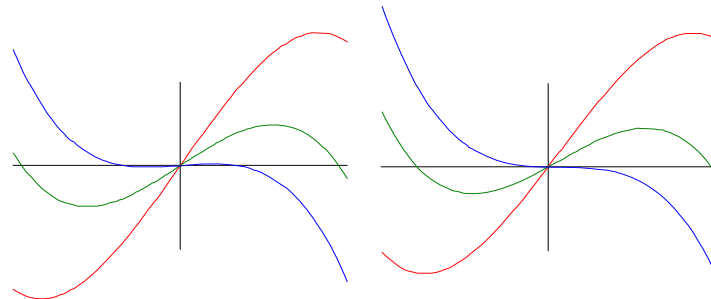
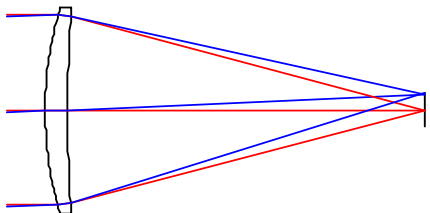
AMTIR-1 singlet (V = 110)

RMS WFE = .209



ZnSe singlet (V = 58)

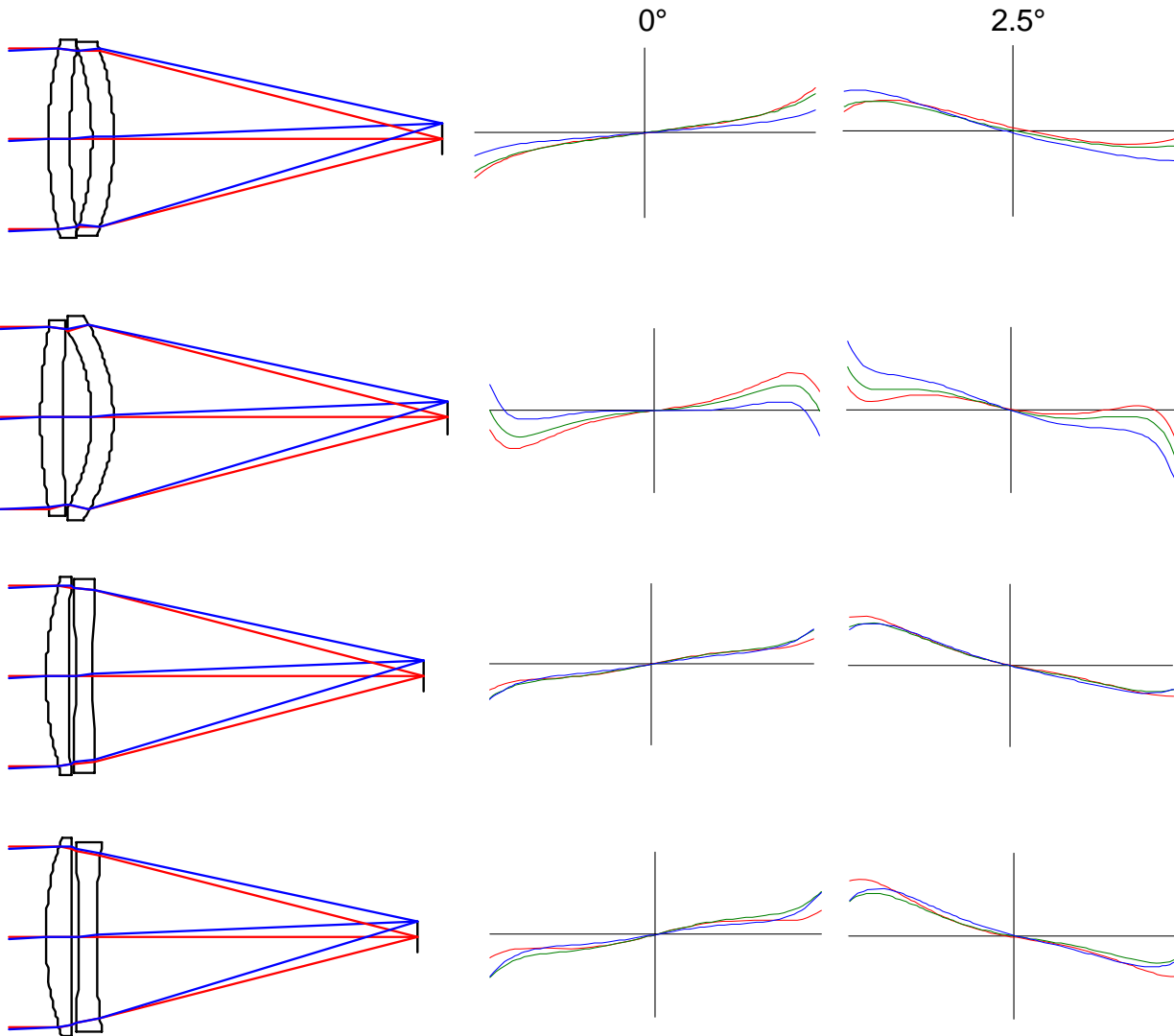
RMS WFE = .331



ZnS singlet (V = 23)

RMS WFE = .769

# Doublet Design Examples – f/2, 50 mm EFL (8 – 12 $\mu$ )



Germanium/ZnS  
RMS WFE = .065

Germanium/AMTIR-1  
RMS WFE = .064

AMTIR-1/ZnS  
RMS WFE = .074

ZnSe/ZnS  
RMS WFE = .079

# Temperature Effects

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- An optical element has two properties which cause changes in optical performance with temperature
  - The **coefficient of thermal expansion**, CTE, usually denoted by  $\alpha$  with units of length/length/°C
  - The **change in refractive index with temperature**  $dn/dT$

- The change in focal length of a lens with temperature is given by

$$\Delta F = F \left( \alpha - \frac{1}{n-1} \frac{dn}{dT} \right) \Delta T$$

- Since in most cases the focal length decreases with temperature, the equation is usually stated as  $\Delta F = -v F \Delta T$  where

$$v = \frac{1}{n-1} \frac{dn}{dT} - \alpha$$

- $v$  is often referred to as the **thermo-optic coefficient**
- The shift in focus relative to the image plane also includes the CTE of the lens mount, so the shift in focus is given by  $\Delta_{\text{focus}} = -(v + \alpha_{\text{mount}}) F \Delta T$

# $\nu$ Values of Optical Materials ( $\times 10^6/^\circ\text{C}$ )

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- **Visible glasses**

|       |       |
|-------|-------|
| BK7   | 1.5   |
| BaK4  | 0.3   |
| BaK50 | -11.4 |
| SK16  | 3.4   |
| SF4   | -3.8  |

It is possible to find combinations of visible glasses to make an athermal design with common mounting materials

- **Infrared glasses**

|           |     |
|-----------|-----|
| Germanium | 127 |
| TI-1173   | 34  |
| ZnS       | 28  |
| ZnSe      | 35  |
| Silicon   | 63  |

Most common IR materials have positive  $\nu$ , so it is more difficult to make a passive athermal design

- **CTE of common mount materials ( $\times 10^6/^\circ\text{C}$ )**

|               |      |
|---------------|------|
| Aluminum 6061 | 23.4 |
| 416 stainless | 9.9  |
| Invar35       | 0.6  |
| Titanium      | 8.7  |
| Beryllium     | 11.6 |

# Example of Temperature Change

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- An IR lens is made of germanium for use at 10 microns
- It has a focal length of 4 inches and an aperture of 2 inches (f/2)
- The diffraction-limited depth of focus is  $\pm 2\lambda f^2 = \pm 0.0032$  inches
- If we mount the lens in an aluminum mount, the change in focus is  $\Delta_{\text{focus}} = 4(-127-23) \times 10^{-6} / ^\circ\text{C} = -0.0006$  in/ $^\circ\text{C}$
- The lens defocus will exceed the diffraction depth of focus over a change in temperature of  $\pm 5^\circ\text{C}$ 
  - Note that for military applications, the operating temperature range is typically  $\pm 50^\circ\text{C}$

# Making an Athermal Doublet

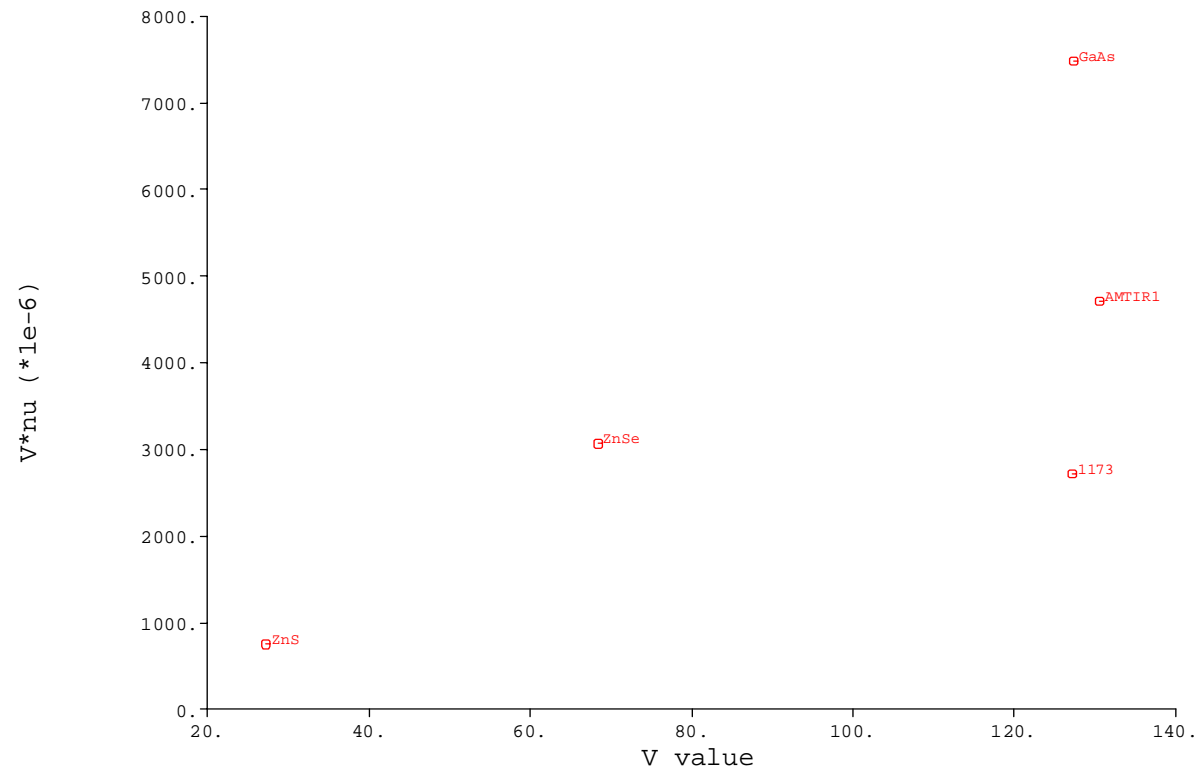
- To satisfy achromatism, the two lenses of a doublet must satisfy the usual achromatic equations

$$f_a = f (V_a - V_b) / V_a$$

$$f_b = f (V_b - V_a) / V_b$$

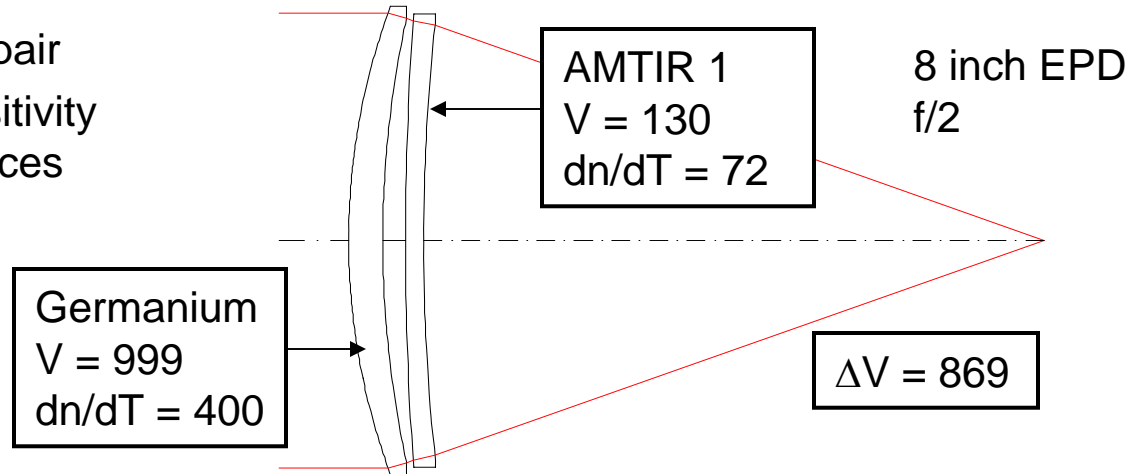
- To be athermalized, the lenses must also satisfy

$$V_a v_a = V_b v_b$$

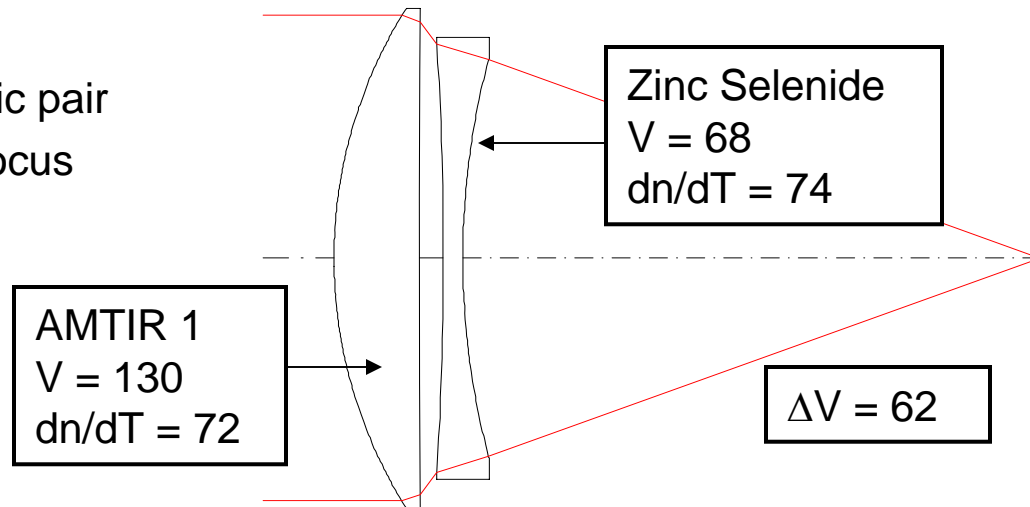


# IR Achromatic Doublet Examples (8 - 11.5 microns)

- Common IR achromatic pair
  - Up to 25% less sensitivity to dispersion tolerances



- Reduced  $dn/dT$  achromatic pair
  - 3X lower change in focus due to temperature



# Infrared Optics Suppliers

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- Elcan Optical Systems, Richardson, TX
- Corning NetOptix, Keene, NH
- Exotic Electro-Optics, Marietta, CA
- Optimum Optical Systems, Camarillo, CA
- II-VI Incorporated, Saxonburg, PA
- Janos Technology, Keene, NH
- DRS Optronics, Palm Bay, FL
- Coherent, Auburn, CA
- Diversified Optical Products, Salem, NH
- Telic OSTI, North Billerica, MA

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