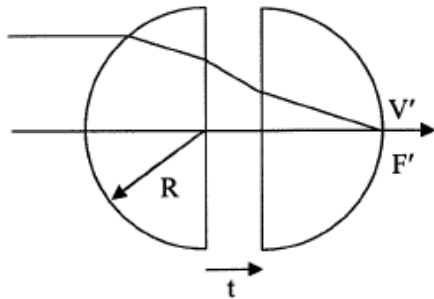


Separated Hemispheres



$$\phi_1 = (1.5 - 1.0) / R$$

$$\phi_1 = 0.01 / \text{mm}$$

The curved surface of the second hemisphere has no optical effect for this problem.

Several solution methods possible.

Solution 1 Determine the BFD of the first hemisphere.

$$\phi_2 = 0 \quad \phi = \phi_1 = 0.01 / \text{mm} \quad f = f'_2 = 1 / \phi = 100 \text{ mm}$$

For the first hemisphere, $n' = 1$

$$d' = -\frac{\phi_1}{\phi} \frac{x}{n} = -\frac{x}{n} = -\frac{R}{1.5} = -\frac{50}{1.5} = -33.33 \text{ mm}$$

$$\text{BFD} = f'_2 + d' = 100 \text{ mm} - 33.33 \text{ mm} = 66.67 \text{ mm}$$

The second hemisphere looks just like a block of glass of thickness R placed after the first hemisphere.

Use reduced thickness: For F' at V' :

$$\text{BFD} = x + \frac{R}{n} = 66.67 \text{ mm}$$

$$x = 66.67 - 33.33 = 33.33 \text{ mm}$$

Solution 2

Consider this situation to be a single refracting surface with a inserted "block" of air.

$$f_1 = \frac{1}{\phi_1} = 100 \text{ mm} \quad \text{Here } n' = 1.5 \text{ for the refracting surface.}$$

$$f_2' = n f_1 = 150 \text{ mm}$$

$$\text{For } F' \text{ at } V': \quad f_2' = R + n d + R = 150 \text{ mm}$$

$$n d = 50 \text{ mm} \quad d = 33.33 \text{ mm}$$

or solve in reduced thicknesses:

$$f = \frac{f_2'}{n} = \frac{R}{n} + d + \frac{R}{n} = 100 \text{ mm}$$

$$d = 33.33 \text{ mm}$$